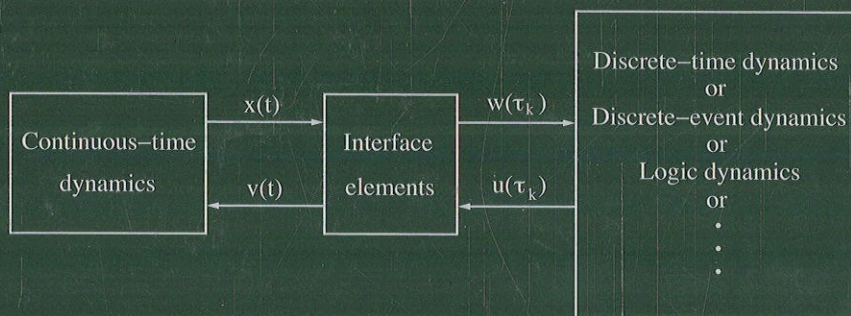


Systems & Control: Foundations & Applications

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Stability of Dynamical Systems

*Continuous, Discontinuous,
and Discrete Systems*



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