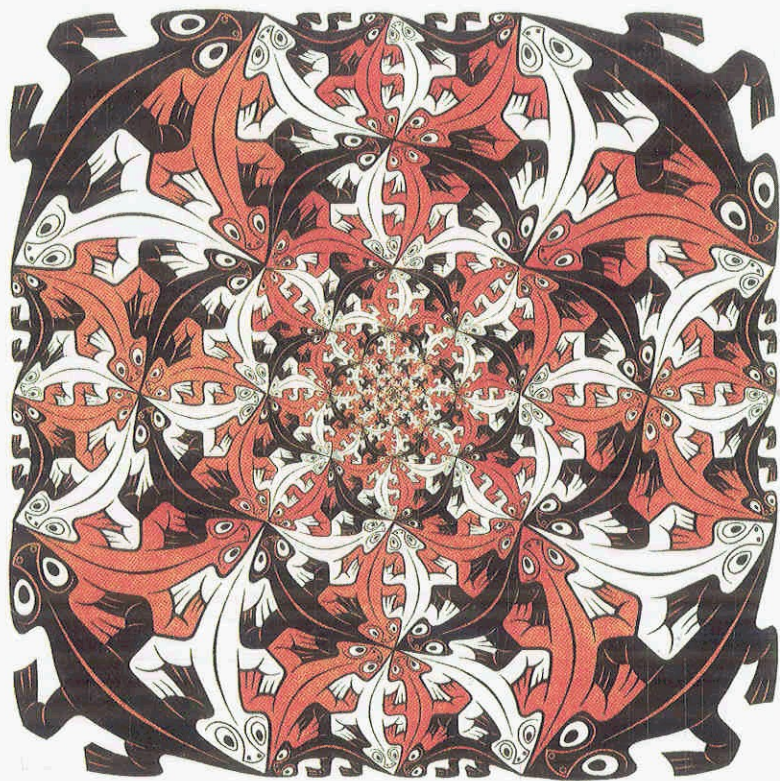


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# Scaling Analysis in Modeling Transport and Reaction Processes



A Systematic Approach to Model  
Building and the Art of Approximation

William B. Krantz

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