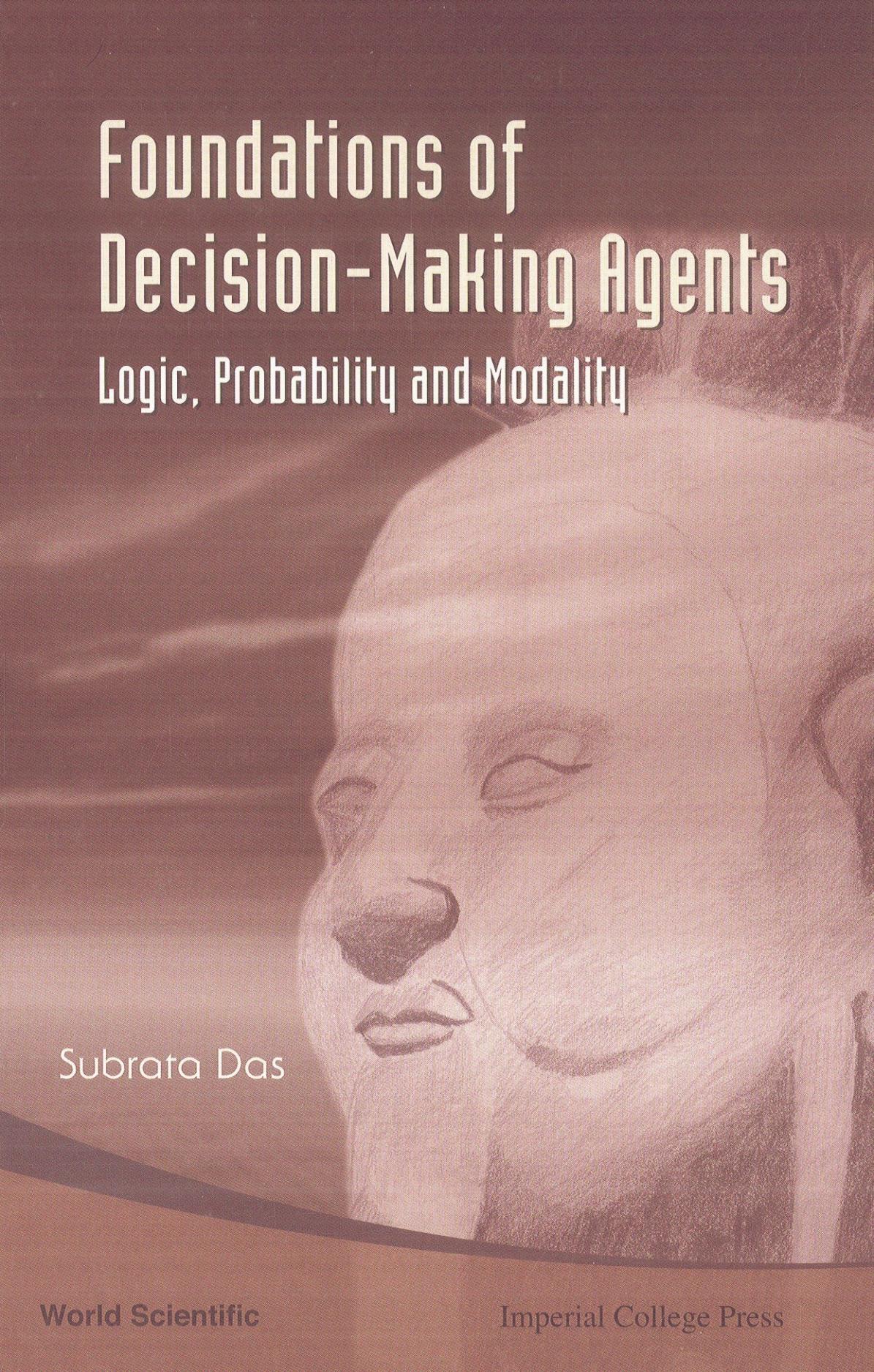


# Foundations of Decision-Making Agents

## Logic, Probability and Modality



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