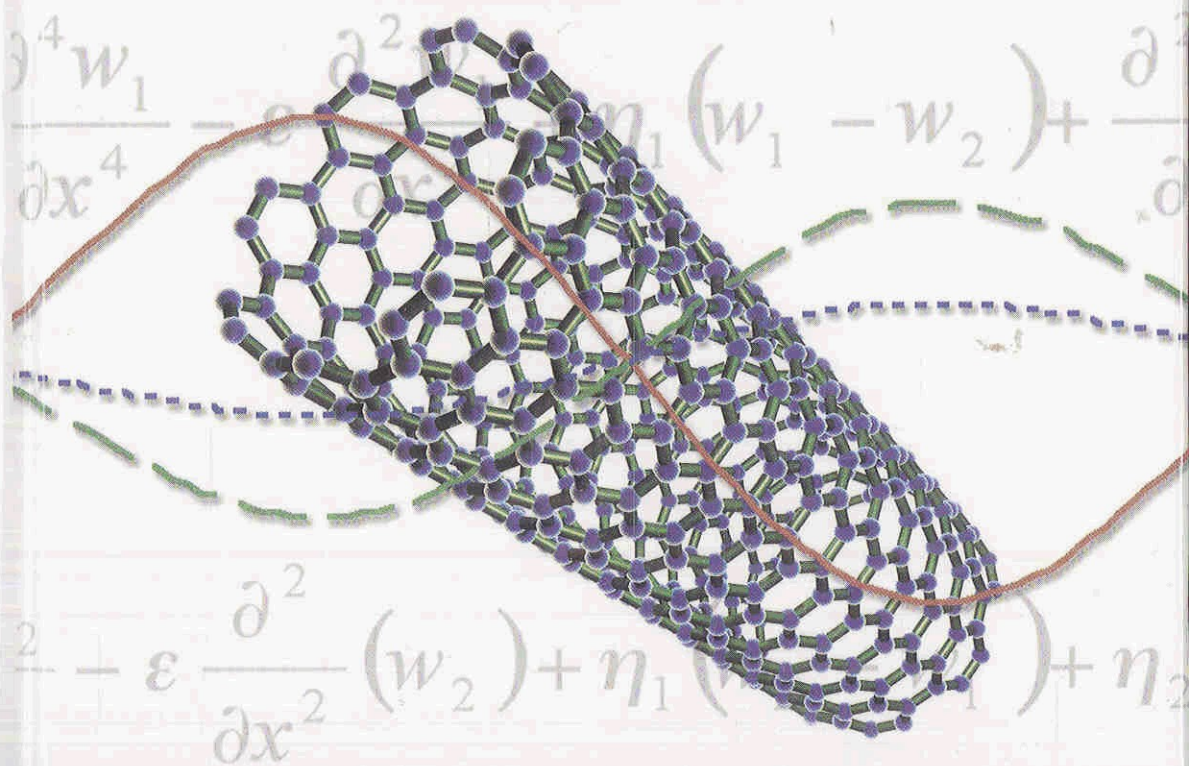


ADVANCED ENGINEERING MATHEMATICS

with Modeling Applications



S. Graham Kelly



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