IMPACT VELOCITY FROM CONSERVATION OF LINEAR MOMENTUM FOR THE

TRAFFIC ACCIDENT INVESTIGATOR AND RECONSTRUCTIONIST

A Manual on Deriving and Using the Speed-at-Impact Equations with the 360 Degree Method

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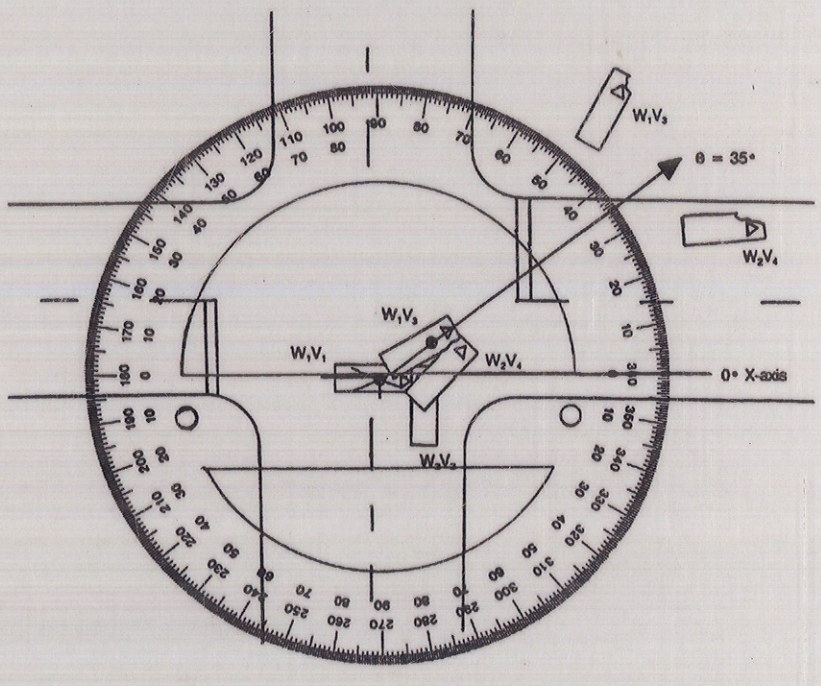

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