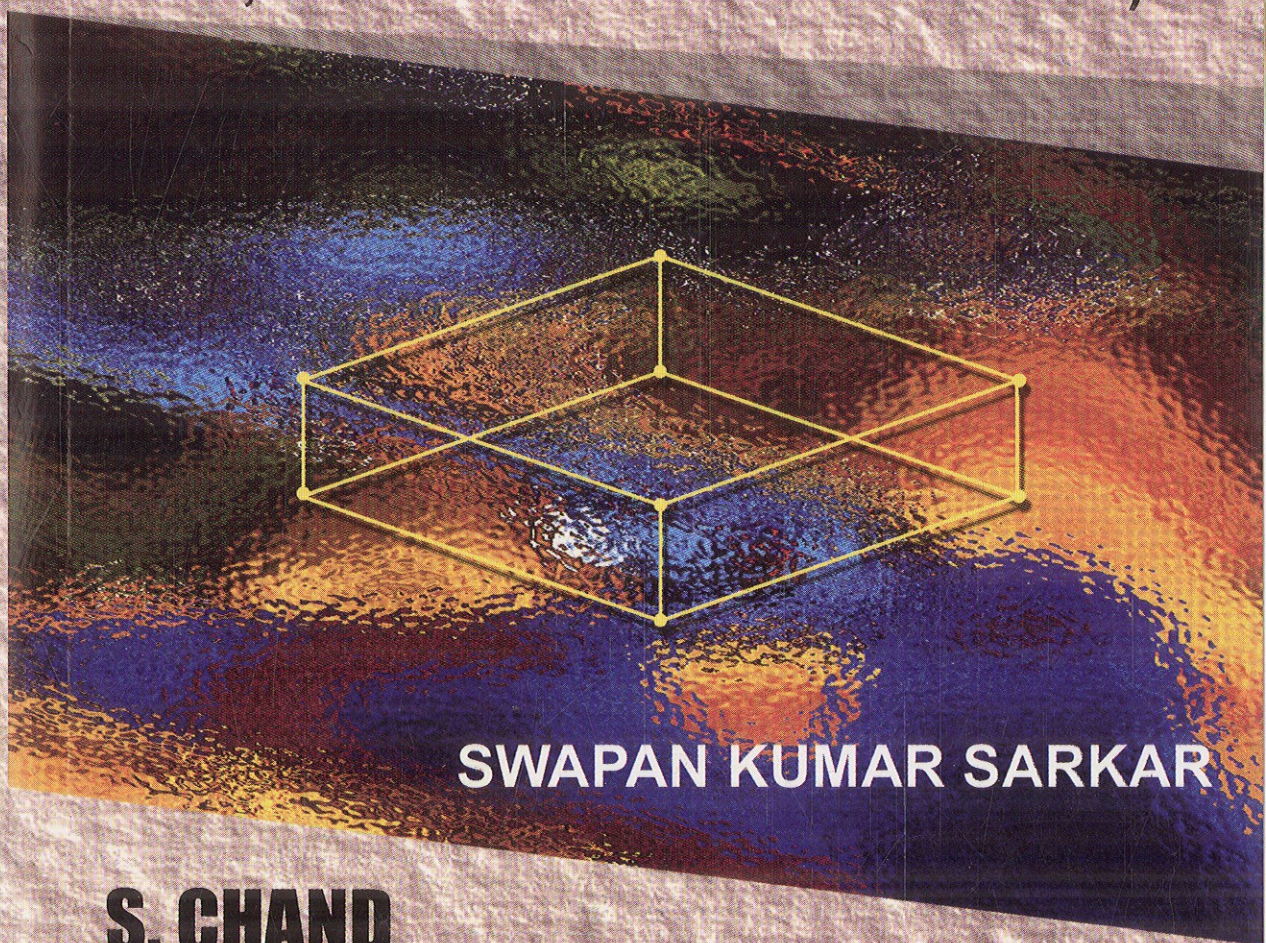
A TEXTBOOK OF
DISCRETE MATHEMATICS

(B.E., B.Tech., B.Sc.(Computer Science), B.I.T., B.C.A. and I.T. related Courses)



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