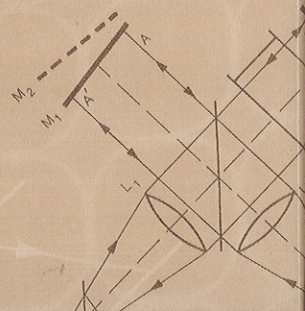
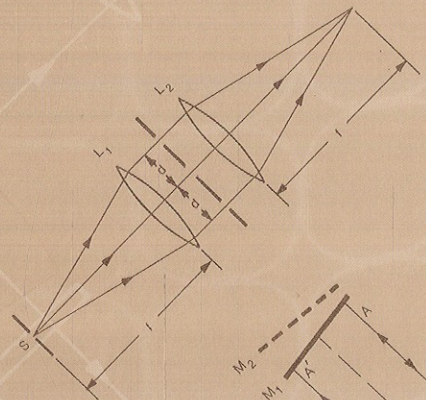
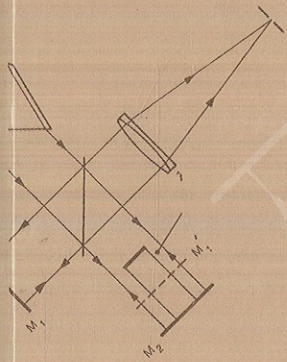


OPTICAL INTERFEROMETRY

S e c o n d E d i t i o n

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