

mp3
MPEG2
H.263
H.264
Wavelets
SPIHT
JPEG-LS
CELP
ppm
BWT
VQ
TCQ
CALIC
MELP

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Introduction to

DATA COMPRESSION

THIRD EDITION

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