

quantitative trait loci analysis in animals

2nd edition

$$L = \prod \left[\frac{1 e^{-(y_i - \mu)^2 / 2\sigma^2}}{\sqrt{2\pi\sigma^2}} \right]$$

$$\text{Log } L = \sum \log \left[\frac{1 e^{-(y_i - \mu)^2 / 2\sigma^2}}{\sqrt{2\pi\sigma^2}} \right]$$

$$d(\text{Log } L)/d\mu =$$



Joel Ira Weller

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