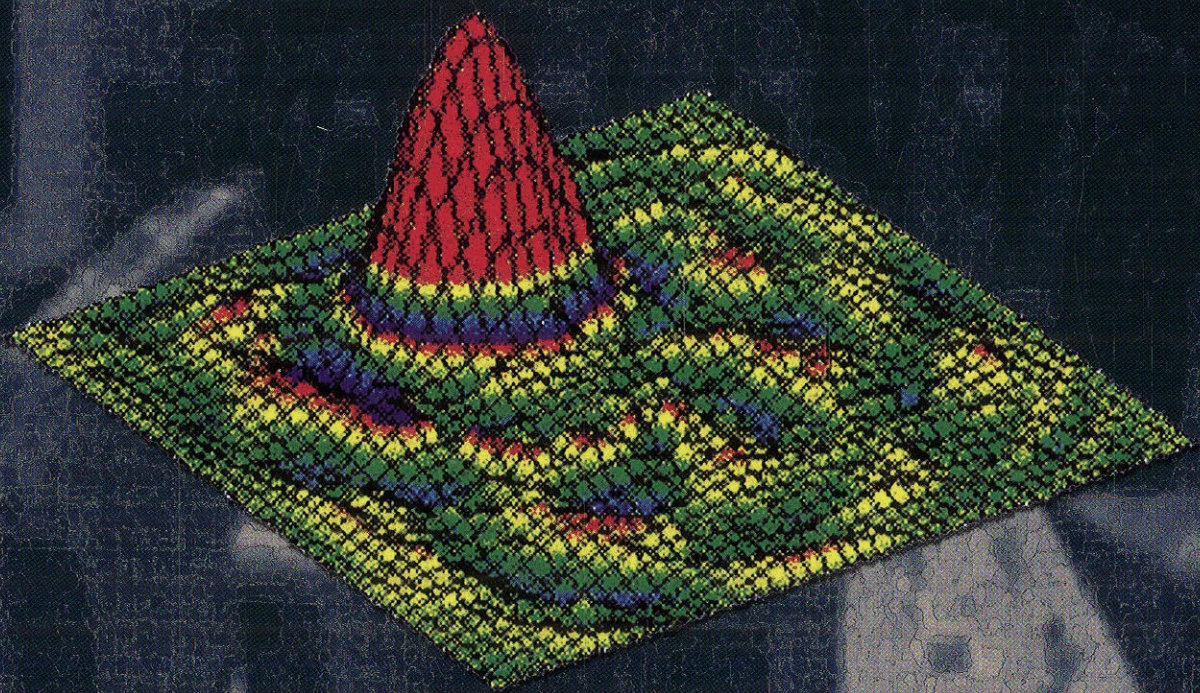


# Parallel Scientific Computing in C++ and MPI

A Seamless Approach to Parallel Algorithms  
and Their Implementation



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