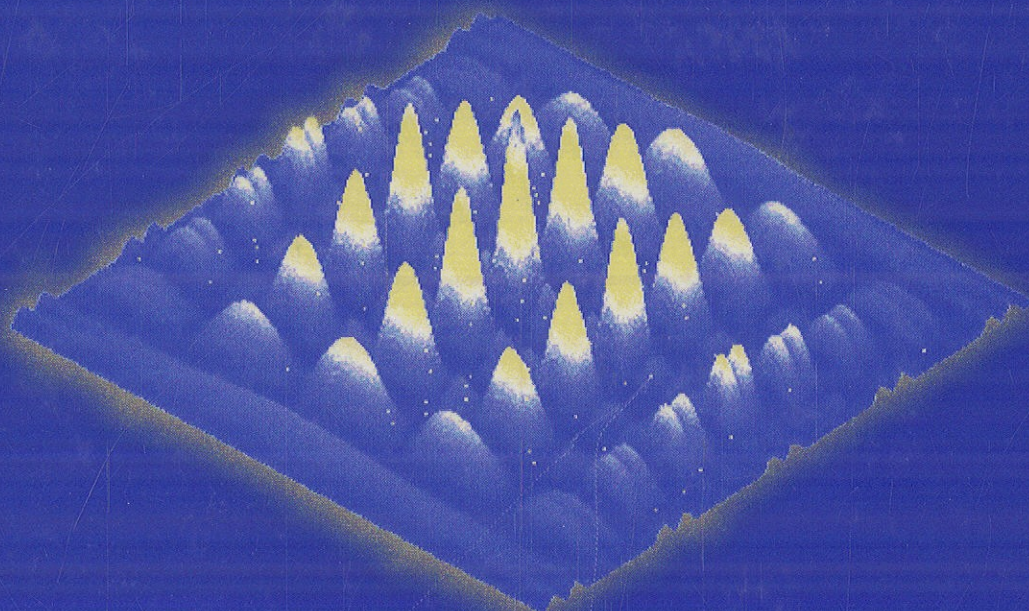


RADAR SIGNAL ANALYSIS AND PROCESSING USING MATLAB®



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MATLAB®
examples



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