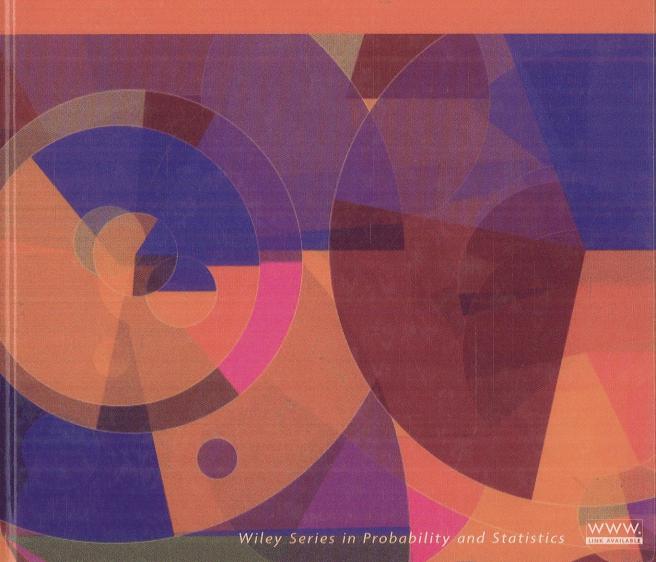


## Approximate Dynamic Programming

Solving the Curses of Dimensionality

Warren B. Powell



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