

Series on Number Theory and Its Applications **Vol. 4**

PROBLEMS AND SOLUTIONS IN REAL ANALYSIS



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Contents

<i>Preface</i>	v
1. Sequences and Limits	1
Solutions	5
2. Infinite Series	15
Solutions	20
3. Continuous Functions	31
Solutions	35
4. Differentiation	43
Solutions	49
5. Integration	59
Solutions	66
6. Improper Integrals	77
Solutions	81
7. Series of Functions	93
Solutions	100
8. Approximation by Polynomials	113
Solutions	117

9.	Convex Functions	125
	Solutions	129
10.	Various proofs of $\zeta(2) = \pi^2/6$	139
	Solutions	146
11.	Functions of Several Variables	157
	Solutions	161
12.	Uniform Distribution	171
	Solutions	174
13.	Rademacher Functions	181
	Solutions	185
14.	Legendre Polynomials	191
	Solutions	195
15.	Chebyshev Polynomials	205
	Solutions	209
16.	Gamma Function	219
	Solutions	225
17.	Prime Number Theorem	239
	Solutions	245
18.	Miscellanies	257
	Solutions	263
	<i>Bibliography</i>	273
	<i>Index</i>	285