



SPRINGER OPTIMIZATION  
AND ITS APPLICATIONS

29

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# Transportation Systems Analysis

Models and Applications

Second Edition



Springer

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