



Statistical Methods in Food and Consumer Research

Second Edition



The background of the book cover features a dark, textured surface with faint, glowing dashed lines and small, glowing circular and star-like shapes. In the lower half, there are several solid, semi-transparent rectangular blocks of varying sizes and colors (brown, green, yellow) that overlap each other, creating a sense of depth and data analysis.

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