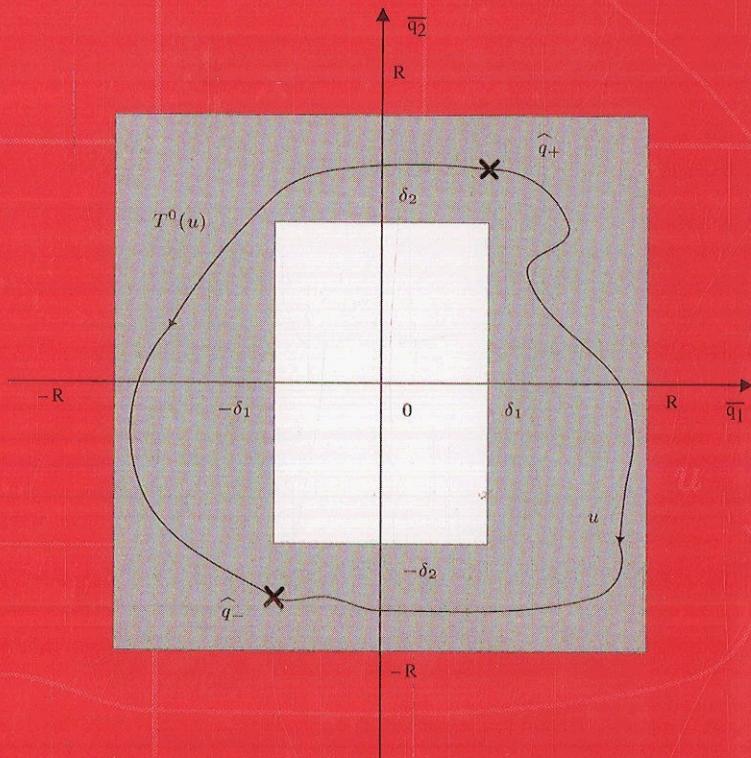


Topological Fixed Point Theory and Its Applications

Fixed Point Theory for Decomposable Sets

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