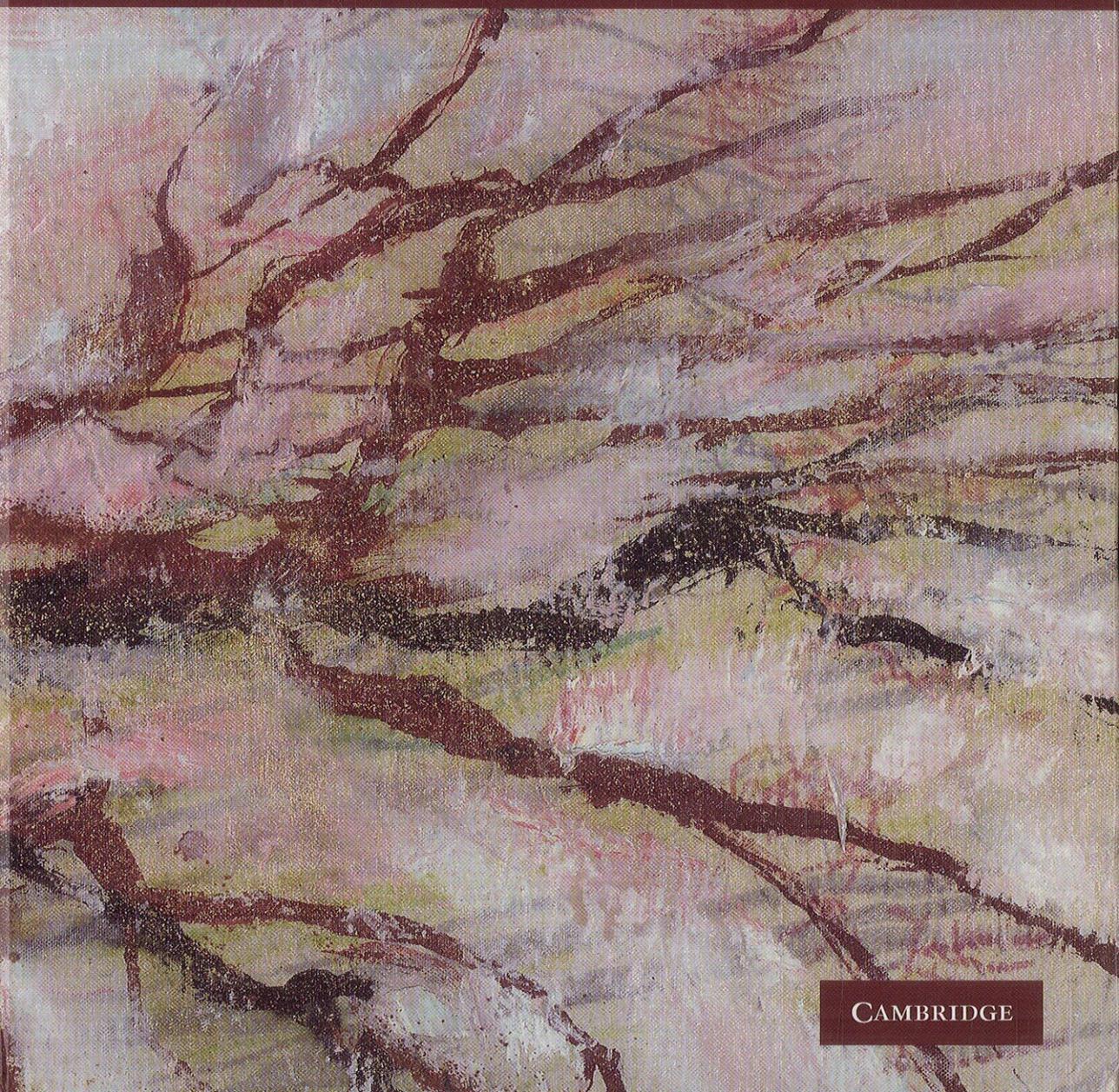


Quantum Statistical Mechanics

William C. Schieve and Lawrence P. Horwitz



CAMBRIDGE

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