



Signals, Systems, Transforms, and Digital Signal Processing with **MATLAB®**

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MATLAB®
examples

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Contents

Preface	xxv
Acknowledgment	xxvii
1 Continuous-Time and Discrete-Time Signals and Systems	1
1.1 Introduction	2
1.2 Continuous-Time Signals	2
1.3 Periodic Functions	3
1.4 Unit Step Function	4
1.5 Graphical Representation of Functions	5
1.6 Even and Odd Parts of a Function	6
1.7 Dirac-Delta Impulse	7
1.8 Basic Properties of the Dirac-Delta Impulse	8
1.9 Other Important Properties of the Impulse	11
1.10 Continuous-Time Systems	11
1.11 Causality, Stability	12
1.12 Examples of Electrical Continuous-Time Systems	12
1.13 Mechanical Systems	13
1.14 Transfer Function and Frequency Response	14
1.15 Convolution and Correlation	15
1.16 A Right-Sided and a Left-Sided Function	20
1.17 Convolution with an Impulse and Its Derivatives	21
1.18 Additional Convolution Properties	21
1.19 Correlation Function	22
1.20 Properties of the Correlation Function	22
1.21 Graphical Interpretation	23
1.22 Correlation of Periodic Functions	25
1.23 Average, Energy and Power of Continuous-Time Signals	25
1.24 Discrete-Time Signals	26
1.25 Periodicity	27
1.26 Difference Equations	28
1.27 Even/Odd Decomposition	28
1.28 Average Value, Energy and Power Sequences	29
1.29 Causality, Stability	30
1.30 Problems	30
1.31 Answers to Selected Problems	40
2 Fourier Series Expansion	47
2.1 Trigonometric Fourier Series	47
2.2 Exponential Fourier Series	48
2.3 Exponential versus Trigonometric Series	50
2.4 Periodicity of Fourier Series	51

2.5	Dirichlet Conditions and Function Discontinuity	53
2.6	Proof of the Exponential Series Expansion	55
2.7	Analysis Interval versus Function Period	55
2.8	Fourier Series as a Discrete-Frequency Spectrum	56
2.9	Meaning of Negative Frequencies	58
2.10	Properties of Fourier Series	58
2.10.1	Linearity	58
2.10.2	Time Shift	60
2.10.3	Frequency Shift	60
2.10.4	Function Conjugate	61
2.10.5	Reflection	61
2.10.6	Symmetry	64
2.10.7	Half-Periodic Symmetry	65
2.10.8	Double Symmetry	67
2.10.9	Time Scaling	70
2.10.10	Differentiation Property	72
2.11	Differentiation of Discontinuous Functions	74
2.11.1	Multiplication in the Time Domain	74
2.11.2	Convolution in the Time Domain	75
2.11.3	Integration	75
2.12	Fourier Series of an Impulse Train	77
2.13	Expansion into Cosine or Sine Fourier Series	78
2.14	Deducing a Function Form from Its Expansion	81
2.15	Truncated Sinusoid Spectral Leakage	83
2.16	The Period of a Composite Sinusoidal Signal	86
2.17	Passage through a Linear System	88
2.18	Parseval's Relations	89
2.19	Use of Power Series Expansion	90
2.20	Inverse Fourier Series	91
2.21	Problems	92
2.22	Answers to Selected Problems	100
3	Laplace Transform	105
3.1	Introduction	105
3.2	Bilateral Laplace Transform	105
3.3	Conditions of Existence of Laplace Transform	107
3.4	Basic Laplace Transforms	110
3.5	Notes on the ROC of Laplace Transform	112
3.6	Properties of Laplace Transform	115
3.6.1	Linearity	116
3.6.2	Differentiation in Time	116
3.6.3	Multiplication by Powers of Time	116
3.6.4	Convolution in Time	117
3.6.5	Integration in Time	117
3.6.6	Multiplication by an Exponential (Modulation)	118
3.6.7	Time Scaling	118
3.6.8	Reflection	119
3.6.9	Initial Value Theorem	119
3.6.10	Final Value Theorem	119
3.6.11	Laplace Transform of Anticausal Functions	120
3.6.12	Shift in Time	121

3.7	Applications of the Differentiation Property	122
3.8	Transform of Right-Sided Periodic Functions	123
3.9	Convolution in Laplace Domain	124
3.10	Cauchy's Residue Theorem	125
3.11	Inverse Laplace Transform	128
3.12	Case of Conjugate Poles	129
3.13	The Expansion Theorem of Heaviside	131
3.14	Application to Transfer Function and Impulse Response	132
3.15	Inverse Transform by Differentiation and Integration	133
3.16	Unilateral Laplace Transform	134
3.16.1	Differentiation in Time	135
3.16.2	Initial and Final Value Theorem	137
3.16.3	Integration in Time Property	137
3.16.4	Division by Time Property	137
3.17	Gamma Function	138
3.18	Table of Additional Laplace Transforms	141
3.19	Problems	143
3.20	Answers to Selected Problems	149
4	Fourier Transform	153
4.1	Definition of the Fourier Transform	153
4.2	Fourier Transform as a Function of f	155
4.3	From Fourier Series to Fourier Transform	156
4.4	Conditions of Existence of the Fourier Transform	157
4.5	Table of Properties of the Fourier Transform	158
4.5.1	Linearity	159
4.5.2	Duality	160
4.5.3	Time Scaling	161
4.5.4	Reflection	161
4.5.5	Time Shift	161
4.5.6	Frequency Shift	161
4.5.7	Modulation Theorem	162
4.5.8	Initial Time Value	163
4.5.9	Initial Frequency Value	163
4.5.10	Differentiation in Time	164
4.5.11	Differentiation in Frequency	164
4.5.12	Integration in Time	164
4.5.13	Conjugate Function	165
4.5.14	Real Functions	165
4.5.15	Symmetry	166
4.6	System Frequency Response	166
4.7	Even–Odd Decomposition of a Real Function	167
4.8	Causal Real Functions	168
4.9	Transform of the Dirac-Delta Impulse	169
4.10	Transform of a Complex Exponential and Sinusoid	169
4.11	Sign Function	171
4.12	Unit Step Function	172
4.13	Causal Sinusoid	172
4.14	Table of Fourier Transforms of Basic Functions	172
4.15	Relation between Fourier and Laplace Transforms	174
4.16	Relation to Laplace Transform with Poles on Imaginary Axis	175

4.17	Convolution in Time	176
4.18	Linear System Input–Output Relation	177
4.19	Convolution in Frequency	178
4.20	Parseval’s Theorem	178
4.21	Energy Spectral Density	179
4.22	Average Value versus Fourier Transform	180
4.23	Fourier Transform of a Periodic Function	181
4.24	Impulse Train	182
4.25	Fourier Transform of Powers of Time	182
4.26	System Response to a Sinusoidal Input	183
4.27	Stability of a Linear System	183
4.28	Fourier Series versus Transform of Periodic Functions	184
4.29	Transform of a Train of Rectangles	184
4.30	Fourier Transform of a Truncated Sinusoid	185
4.31	Gaussian Function Laplace and Fourier Transform	186
4.32	Inverse Transform by Series Expansion	187
4.33	Fourier Transform in ω and f	188
4.34	Fourier Transform of the Correlation Function	189
4.35	Ideal Filters Impulse Response	190
4.36	Time and Frequency Domain Sampling	191
4.37	Ideal Sampling	191
4.38	Reconstruction of a Signal from its Samples	193
4.39	Other Sampling Systems	195
4.39.1	Natural Sampling	195
4.39.2	Instantaneous Sampling	197
4.40	Ideal Sampling of a Bandpass Signal	200
4.41	Sampling an Arbitrary Signal	201
4.42	Sampling the Fourier Transform	203
4.43	Problems	204
4.44	Answers to Selected Problems	222
5	System Modeling, Time and Frequency Response	233
5.1	Transfer Function	233
5.2	Block Diagram Reduction	233
5.3	Galvanometer	234
5.4	DC Motor	237
5.5	A Speed-Control System	239
5.6	Homology	245
5.7	Transient and Steady-State Response	247
5.8	Step Response of Linear Systems	248
5.9	First Order System	248
5.10	Second Order System Model	249
5.11	Settling Time	250
5.12	Second Order System Frequency Response	253
5.13	Case of a Double Pole	254
5.14	The Over-Damped Case	255
5.15	Evaluation of the Overshoot	255
5.16	Causal System Response to an Arbitrary Input	256
5.17	System Response to a Causal Periodic Input	257
5.18	Response to a Causal Sinusoidal Input	259
5.19	Frequency Response Plots	260

5.20	Decibels, Octaves, Decades	260
5.21	Asymptotic Frequency Response	261
5.21.1	A Simple Zero at the Origin	261
5.21.2	A Simple Pole	262
5.21.3	A Simple Zero in the Left Plane	262
5.21.4	First Order System	264
5.21.5	Second Order System	264
5.22	Bode Plot of a Composite Linear System	267
5.23	Graphical Representation of a System Function	268
5.24	Vectorial Evaluation of Residues	269
5.25	Vectorial Evaluation of the Frequency Response	273
5.26	A First Order All-Pass System	275
5.27	Filtering Properties of Basic Circuits	275
5.28	Lowpass First Order Filter	277
5.29	Minimum Phase Systems	280
5.30	General Order All-Pass Systems	281
5.31	Signal Generation	283
5.32	Application of Laplace Transform to Differential Equations	284
5.32.1	Linear Differential Equations with Constant Coefficients	285
5.32.2	Linear First Order Differential Equation	285
5.32.3	General Order Differential Equations with Constant Coefficients	286
5.32.4	Homogeneous Linear Differential Equations	287
5.32.5	The General Solution of a Linear Differential Equation	288
5.32.6	Partial Differential Equations	291
5.33	Transformation of Partial Differential Equations	293
5.34	Problems	297
5.35	Answers to Selected Problems	314
6	Discrete-Time Signals and Systems	323
6.1	Introduction	323
6.2	Linear Time-Invariant Systems	324
6.3	Linear Constant-Coefficient Difference Equations	324
6.4	The z -Transform	325
6.5	Convergence of the z -Transform	327
6.6	Inverse z -Transform	330
6.7	Inverse z -Transform by Partial Fraction Expansion	336
6.8	Inversion by Long Division	337
6.9	Inversion by a Power Series Expansion	338
6.10	Inversion by Geometric Series Summation	339
6.11	Table of Basic z -Transforms	340
6.12	Properties of the z -Transform	340
6.12.1	Linearity	340
6.12.2	Time Shift	340
6.12.3	Conjugate Sequence	340
6.12.4	Initial Value	341
6.12.5	Convolution in Time	344
6.12.6	Convolution in Frequency	344
6.12.7	Parseval's Relation	347
6.12.8	Final Value Theorem	347
6.12.9	Multiplication by an Exponential	348
6.12.10	Frequency Translation	348

6.12.11	Reflection Property	349
6.12.12	Multiplication by n	349
6.13	Geometric Evaluation of Frequency Response	349
6.14	Comb Filters	351
6.15	Causality and Stability	353
6.16	Delayed Response and Group Delay	354
6.17	Discrete-Time Convolution and Correlation	355
6.18	Discrete-Time Correlation in One Dimension	357
6.19	Convolution and Correlation as Multiplications	360
6.20	Response of a Linear System to a Sinusoid	361
6.21	Notes on the Cross-Correlation of Sequences	361
6.22	LTI System Input/Output Correlation Sequences	362
6.23	Energy and Power Spectral Density	363
6.24	Two-Dimensional Signals	363
6.25	Linear Systems, Convolution and Correlation	366
6.26	Correlation of Two-Dimensional Signals	370
6.27	IIR and FIR Digital Filters	374
6.28	Discrete-Time All-Pass Systems	375
6.29	Minimum-Phase and Inverse System	378
6.30	Unilateral z -Transform	381
6.30.1	Time Shift Property of Unilateral z -Transform	383
6.31	Problems	384
6.32	Answers to Selected Problems	390
7	Discrete-Time Fourier Transform	395
7.1	Laplace, Fourier and z -Transform Relations	395
7.2	Discrete-Time Processing of Continuous-Time Signals	400
7.3	A/D Conversion	400
7.4	Quantization Error	403
7.5	D/A Conversion	404
7.6	Continuous versus Discrete Signal Processing	406
7.7	Interlacing with Zeros	407
7.8	Sampling Rate Conversion	409
7.8.1	Sampling Rate Reduction	410
7.8.2	Sampling Rate Increase: Interpolation	414
7.8.3	Rational Factor Sample Rate Alteration	417
7.9	Fourier Transform of a Periodic Sequence	419
7.10	Table of Discrete-Time Fourier Transforms	420
7.11	Reconstruction of the Continuous-Time Signal	424
7.12	Stability of a Linear System	425
7.13	Table of Discrete-Time Fourier Transform Properties	425
7.14	Parseval's Theorem	425
7.15	Fourier Series and Transform Duality	426
7.16	Discrete Fourier Transform	429
7.17	Discrete Fourier Series	433
7.18	DFT of a Sinusoidal Signal	434
7.19	Deducing the z -Transform from the DFT	436
7.20	DFT versus DFS	438
7.21	Properties of DFS and DFT	439
7.21.1	Periodic Convolution	441
7.22	Circular Convolution	443

7.23	Circular Convolution Using the DFT	445
7.24	Sampling the Spectrum	446
7.25	Table of Properties of DFS	447
7.26	Shift in Time and Circular Shift	448
7.27	Table of DFT Properties	449
7.28	Zero Padding	450
7.29	Discrete z -Transform	453
7.30	Fast Fourier Transform	455
7.31	An Algorithm for a Wired-In Radix-2 Processor	462
7.31.1	Post-Permutation Algorithm	464
7.31.2	Ordered Input/Ordered Output (OIOO) Algorithm	465
7.32	Factorization of the FFT to a Higher Radix	466
7.32.1	Ordered Input/Ordered Output General Radix FFT Algorithm	469
7.33	Feedback Elimination for High-Speed Signal Processing	470
7.34	Problems	472
7.35	Answers to Selected Problems	478
8	State Space Modeling	483
8.1	Introduction	483
8.2	Note on Notation	483
8.3	State Space Model	484
8.4	System Transfer Function	488
8.5	System Response with Initial Conditions	489
8.6	Jordan Canonical Form of State Space Model	490
8.7	Eigenvalues and Eigenvectors	497
8.8	Matrix Diagonalization	498
8.9	Similarity Transformation of a State Space Model	499
8.10	Solution of the State Equations	501
8.11	General Jordan Canonical Form	507
8.12	Circuit Analysis by Laplace Transform and State Variables	509
8.13	Trajectories of a Second Order System	513
8.14	Second Order System Modeling	515
8.15	Transformation of Trajectories between Planes	519
8.16	Discrete-Time Systems	522
8.17	Solution of the State Equations	528
8.18	Transfer Function	528
8.19	Change of Variables	529
8.20	Second Canonical Form State Space Model	531
8.21	Problems	533
8.22	Answers to Selected Problems	538
9	Filters of Continuous-Time Domain	543
9.1	Lowpass Approximation	543
9.2	Butterworth Approximation	544
9.3	Denormalization of Butterworth Filter Prototype	547
9.4	Denormalized Transfer Function	550
9.5	The Case $\varepsilon \neq 1$	552
9.6	Butterworth Filter Order Formula	553
9.7	Nomographs	554
9.8	Chebyshev Approximation	556
9.9	Pass-Band Ripple	560

9.10	Transfer Function of the Chebyshev Filter	560
9.11	Maxima and Minima of Chebyshev Filter Response	563
9.12	The Value of ε as a Function of Pass-Band Ripple	564
9.13	Evaluation of Chebyshev Filter Gain	564
9.14	Chebyshev Filter Tables	565
9.15	Chebyshev Filter Order	567
9.16	Denormalization of Chebyshev Filter Prototype	568
9.17	Chebyshev's Approximation: Second Form	571
9.18	Response Decay of Butterworth and Chebyshev Filters	572
9.19	Chebyshev Filter Nomograph	575
9.20	Elliptic Filters	576
9.20.1	Elliptic Integral	576
9.21	Properties, Poles and Zeros of the sn Function	577
9.21.1	Elliptic Filter Approximation	580
9.22	Pole Zero Alignment and Mapping of Elliptic Filter	584
9.23	Poles of $H(s)$	589
9.24	Zeros and Poles of $G(\omega)$	591
9.25	Zeros, Maxima and Minima of the Magnitude Spectrum	591
9.26	Points of Maxima/Minima	591
9.27	Elliptic Filter Nomograph	592
9.28	$N = 9$ Example	597
9.29	Tables of Elliptic Filters	599
9.30	Bessel's Constant Delay Filters	611
9.31	A Note on Continued Fraction Expansion	612
9.32	Evaluating the Filter Delay	617
9.33	Bessel Filter Quality Factor and Natural Frequency	618
9.34	Maximal Flatness of Bessel and Butterworth Response	619
9.35	Bessel Filter's Delay and Magnitude Response	622
9.36	Denormalization and Deviation from Ideal Response	622
9.37	Bessel Filter's Magnitude and Delay	626
9.38	Bessel Filter's Butterworth Asymptotic Form	626
9.39	Delay of Bessel–Butterworth Asymptotic Form Filter	628
9.40	Dclay Plots of Butterworth Asymptotic Form Bessel Filter	629
9.41	Bessel Filters Frequency Normalized Form	633
9.42	Poles and Zeros of Asymptotic and Frequency Normalized Bessel Filter Forms	634
9.43	Response and Delay of Normalized Form Bessel Filter	634
9.44	Bessel Frequency Normalized Form Attenuation Setting	635
9.45	Bessel Filter Nomograph	639
9.46	Frequency Transformations	639
9.47	Lowpass to Bandpass Transformation	641
9.48	Lowpass to Band-Stop Transformation	651
9.49	Lowpass to Highpass Transformation	653
9.50	Note on Lowpass to Normalized Band-Stop Transformation	657
9.51	Windows	661
9.52	Rectangular Window	662
9.53	Triangle (Bartlett) Window	663
9.54	Hanning Window	663
9.55	Hamming Window	664
9.56	Problems	665
9.57	Answers to Selected Problems	671

10 Passive and Active Filters	677
10.1 Design of Passive Filters	677
10.2 Design of Passive Ladder Lowpass Filters	677
10.3 Analysis of a General Order Passive Ladder Network	680
10.4 Input Impedance of a Single-Resistance Terminated Network	683
10.5 Evaluation of the Ladder Network Components	684
10.6 Matrix Evaluation of Input Impedance	689
10.7 Bessel Filter Passive Ladder Networks	693
10.8 Tables of Single-Resistance Ladder Network Components	694
10.9 Design of Doubly Terminated Passive LC Ladder Networks	695
10.9.1 Input Impedance Evaluation	695
10.10 Tables of Double-Resistance Terminated Ladder Network Components . .	701
10.11 Closed Forms for Circuit Element Values	703
10.12 Elliptic Filter Realization as a Passive Ladder Network	706
10.12.1 Evaluating the Elliptic LC Ladder Circuit Elements	707
10.13 Table of Elliptic Filter Passive Network Components	709
10.14 Element Replacement for Frequency Transformation	709
10.14.1 Lowpass to Bandpass Transformation	710
10.14.2 Lowpass to Highpass Transformation	711
10.14.3 Lowpass to Band-Stop Transformation	711
10.15 Realization of a General Order Active Filter	713
10.16 Inverting Integrator	713
10.17 Biquadratic Transfer Functions	714
10.18 General Biquad Realization	716
10.19 First Order Filter Realization	721
10.20 A Biquadratic Transfer Function Realization	723
10.21 Sallen-Key Circuit	725
10.22 Problems	728
10.23 Answers to Selected Problems	729
11 Digital Filters	733
11.1 Introduction	733
11.2 Signal Flow Graphs	733
11.3 IIR Filter Models	734
11.4 First Canonical Form	734
11.5 Transposition	734
11.6 Second Canonical Form	736
11.7 Transposition of the Second Canonical Form	737
11.8 Structures Based on Poles and Zeros	738
11.9 Cascaded Form	738
11.10 Parallel Form	739
11.11 Matrix Representation	739
11.12 Finite Impulse Response (FIR) Filters	740
11.13 Linear Phase FIR Filters	741
11.14 Conversion of Continuous-Time to Discrete-Time Filter	743
11.15 Impulse Invariance Approach	743
11.16 Shortcut Impulse Invariance Design	746
11.17 Backward-Rectangular Approximation	747
11.18 Forward Rectangular and Trapezoidal Approximations	749
11.19 Bilinear Transform	751
11.20 Lattice Filters	760

11.21	Finite Impulse Response All-Zero Lattice Structures	760
11.22	One-Zero FIR Filter	761
11.23	Two-Zeros FIR Filter	762
11.24	General Order All-Zero FIR Filter	764
11.25	All-Pole Filter	769
11.26	First Order One-Pole Filter	770
11.27	Second Order All-Pole Filter	771
11.28	General Order All-Pole Filter	772
11.29	Pole-Zero IIR Lattice Filter	775
11.30	All-Pass Filter Realization	781
11.31	Schur–Cohn Stability Criterion	782
11.32	Frequency Transformations	783
11.33	Least Squares Digital Filter Design	786
11.34	Padé Approximation	786
11.35	Error Minimization in Prony's Method	790
11.36	FIR Inverse Filter Design	794
11.37	Impulse Response of Ideal Filters	798
11.38	Spectral Leakage	800
11.39	Windows	801
11.40	Ideal Digital Filters Rectangular Window	801
11.41	Hanning Window	802
11.42	Hamming Window	803
11.43	Triangular Window	804
11.44	Comparison of Windows Spectral Parameters	805
11.45	Linear-Phase FIR Filter Design Using Windows	807
11.46	Even- and Odd-Symmetric FIR Filter Design	808
11.47	Linear Phase FIR Filter Realization	810
11.48	Sampling the Unit Circle	810
11.49	Impulse Response Evaluation from Unit Circle Samples	814
11.49.1	Case I-1: Odd Order, Even Symmetry, $\mu = 0$	814
11.49.2	Case I-2: Odd Order, Even Symmetry, $\mu = 1/2$	815
11.49.3	Case II-1	815
11.49.4	Case II-2: Even Order, Even Symmetry, $\mu = 1/2$	815
11.49.5	Case III-1: Odd Order, Odd Symmetry, $\mu = 0$	816
11.49.6	Case III-2: Odd Order, Odd Symmetry, $\mu = 1/2$	816
11.49.7	Case IV-1: Even Order, Odd Symmetry, $\mu = 0$	816
11.49.8	Case IV-2: Even Order, Odd Symmetry, $\mu = 1/2$	816
11.50	Problems	817
11.51	Answers to Selected Problems	828
12	Energy and Power Spectral Densities	835
12.1	Energy Spectral Density	835
12.2	Average, Energy and Power of Continuous-Time Signals	838
12.3	Discrete-Time Signals	839
12.4	Energy Signals	840
12.5	Autocorrelation of Energy Signals	840
12.6	Energy Signal through Linear System	842
12.7	Impulsive and Discrete-Time Energy Signals	843
12.8	Power Signals	848
12.9	Cross-Correlation	848
12.9.1	Power Spectral Density	849

12.10	Power Spectrum Conversion of a Linear System	850
12.11	Impulsive and Discrete-Time Power Signals	852
12.12	Periodic Signals	854
12.12.1	Response of an LTI System to a Sinusoidal Input	855
12.13	Power Spectral Density of an Impulse Train	856
12.14	Average, Energy and Power of a Sequence	859
12.15	Energy Spectral Density of a Sequence	860
12.16	Autocorrelation of an Energy Sequence	860
12.17	Power Density of a Sequence	860
12.18	Passage through a Linear System	861
12.19	Problems	861
12.20	Answers to Selected Problems	869
13	Introduction to Communication Systems	875
13.1	Introduction	875
13.2	Amplitude Modulation (AM) of Continuous-Time Signals	876
13.2.1	Double Side-Band (DSB) Modulation	876
13.2.2	Double Side-Band Suppressed Carrier (DSB-SC) Modulation	877
13.2.3	Single Side-Band (SSB) Modulation	879
13.2.4	Vestigial Side-Band (VSB) Modulation	882
13.2.5	Frequency Multiplexing	882
13.3	Frequency Modulation	883
13.4	Discrete Signals	887
13.4.1	Pulse Modulation Systems	887
13.5	Digital Communication Systems	888
13.5.1	Pulse Code Modulation	888
13.5.2	Pulse Duration Modulation	890
13.5.3	Pulse Position Modulation	892
13.6	PCM-TDM Systems	893
13.7	Frequency Division Multiplexing (FDM)	893
13.8	Problems	894
13.9	Answers to Selected Problems	904
14	Fourier-, Laplace- and z-Related Transforms	911
14.1	Walsh Transform	911
14.2	Rademacher and Haar Functions	911
14.3	Walsh Functions	912
14.4	The Walsh (Seqency) Order	913
14.5	Dyadic (Paley) Order	914
14.6	Natural (Hadamard) Order	914
14.7	Discrete Walsh Transform	916
14.8	Discrete-Time Walsh Transform	917
14.9	Discrete-Time Walsh–Hadamard Transform	917
14.9.1	Natural (Hadamard) Order	917
14.9.2	Dyadic or Paley Order	918
14.9.3	Seqency or Walsh Order	919
14.10	Natural (Hadamard) Order Fast Walsh Hadamard Transform	919
14.11	Dyadic (Paley) Order Fast Walsh–Hadamard Transform	920
14.12	Seqency Ordered Fast Walsh–Hadamard Transform	921
14.13	Generalized Walsh Transform	922
14.14	Natural Order	922

14.15	Generalized Sequency Order	923
14.16	Generalized Walsh–Paley (p-adic) Transform	923
14.17	Walsh–Kaczmarz Transform	923
14.18	Generalized Walsh Factorizations for Parallel Processing	924
14.19	Generalized Walsh Natural Order GWN Matrix	924
14.20	Generalized Walsh–Paley GWP Transformation Matrix	925
14.21	GWK Transformation Matrix	926
14.22	High Speed Optimal Generalized Walsh Factorizations	926
14.23	GWN Optimal Factorization	926
14.24	GWP Optimal Factorization	927
14.25	GWK Optimal Factorization	927
14.26	Karhunen Loève Transform	928
14.27	Hilbert Transform	931
14.28	Hilbert Transformer	934
14.29	Discrete Hilbert Transform	935
14.30	Hartley Transform	936
14.31	Discrete Hartley Transform	938
14.32	Mellin Transform	939
14.33	Mellin Transform of e^{jx}	941
14.34	Hankel Transform	943
14.35	Fourier Cosine Transform	945
14.36	Discrete Cosine Transform (DCT)	946
14.37	Fractional Fourier Transform	948
14.38	Discrete Fractional Fourier Transform	950
14.39	Two-Dimensional Transforms	950
14.40	Two-Dimensional Fourier Transform	951
14.41	Continuous-Time Domain Hilbert Transform Relations	953
14.42	$H_I(j\omega)$ versus $H_R(j\omega)$ with No Poles on Axis	953
14.43	Case of Poles on the Imaginary Axis	957
14.44	Hilbert Transform Closed Forms	958
14.45	Wiener–Lee Transforms	959
14.46	Discrete-Time Domain Hilbert Transform Relations	961
14.47	Problems	964
14.48	Answers to Selected Problems	967
15	Digital Signal Processors: Architecture, Logic Design	973
15.1	Introduction	973
15.2	Systems for the Representation of Numbers	973
15.3	Conversion from Decimal to Binary	974
15.4	Integers, Fractions and the Binary Point	974
15.5	Representation of Negative Numbers	975
15.5.1	Sign and Magnitude Notation	975
15.5.2	1's and 2's Complement Notation	976
15.6	Integer and Fractional Representation of Signed Numbers	978
15.6.1	1's and 2's Complement of Signed Numbers	979
15.7	Addition	982
15.7.1	Addition in Sign and Magnitude Notation	982
15.7.2	Addition in 1's Complement Notation	984
15.7.3	Addition in 2's Complement Notation	985
15.8	Subtraction	986
15.8.1	Subtraction in Sign and Magnitude Notation	987

15.8.2	Numbers in 1's Complement Notation	988
15.8.3	Subtraction in 2's Complement Notation	989
15.9	Full Adder Cell	990
15.10	Addition/Subtraction Implementation in 2's Complement	991
15.11	Controlled Add/Subtract (CAS) Cell	992
15.12	Multiplication of Unsigned Numbers	992
15.13	Multiplier Implementation	993
15.14	3-D Multiplier	995
15.14.1	Multiplication in Sign and Magnitude Notation	997
15.14.2	Multiplication in 1's Complement Notation	997
15.14.3	Numbers in 2's Complement Notation	998
15.15	A Direct Approach to 2's Complement Multiplication	1000
15.16	Division	1002
15.16.1	Division of Positive Numbers:	1003
15.16.2	Division in Sign and Magnitude Notation	1004
15.16.3	Division in 1's Complement	1004
15.16.4	Division in 2's Complement	1005
15.16.5	Nonrestoring Division	1006
15.17	Cellular Array for Nonrestoring Division	1009
15.18	Carry Look Ahead (CLA) Cell	1011
15.19	2's Complement Nonrestoring Division	1014
15.20	Convergence Division	1016
15.21	Evaluation of the n^{th} Root	1018
15.22	Function Generation by Chebyshev Series Expansion	1020
15.23	An Alternative Approach to Chebyshev Series Expansion	1026
15.24	Floating Point Number Representation	1027
15.24.1	Addition and Subtraction	1029
15.24.2	Multiplication	1029
15.24.3	Division	1030
15.25	Square Root Evaluation	1030
15.25.1	The Paper and Pencil Method	1030
15.25.2	Binary Square Root Evaluation	1031
15.25.3	Comparison Approach	1031
15.25.4	Restoring Approach	1032
15.25.5	Nonrestoring Approach	1032
15.26	Cellular Array for Nonrestoring Square Root Extraction	1033
15.27	Binary Coded Decimal (BCD) Representation	1033
15.28	Memory Elements	1037
15.28.1	Set-Reset (SR) Flip-Flop	1038
15.28.2	The Trigger or T Flip-Flop	1040
15.28.3	The JK Flip-Flop	1040
15.28.4	Master-Slave Flip-Flop	1041
15.29	Design of Synchronous Sequential Circuits	1042
15.29.1	Realization Using SR Flip-Flops	1044
15.29.2	Realization Using JK Flip-Flops.	1045
15.30	Realization of a Counter Using T Flip-Flops	1046
15.30.1	Realization Using JK Flip-Flops	1046
15.31	State Minimization	1048
15.32	Asynchronous Sequential Machines	1050
15.33	State Reduction	1051
15.34	Control Counter Design for Generator of Prime Numbers	1054

15.34.1 Micro-operations and States	1055
15.35 Fast Transform Processors	1059
15.36 Programmable Logic Arrays (PLAs)	1062
15.37 Field Programmable Gate Arrays (FPGAs)	1063
15.38 DSP with Xilinx FPGAs	1065
15.39 Texas Instruments TMS320C6713B Floating-Point DSP	1067
15.40 Central Processing Unit (CPU)	1069
15.41 CPU Data Paths and Control	1071
15.41.1 General-Purpose Register Files	1071
15.41.2 Functional Units	1072
15.41.3 Register File Cross Paths	1072
15.41.4 Memory, Load, and Store Paths	1073
15.41.5 Data Address Paths	1073
15.42 Instruction Syntax	1074
15.43 TMS320C6000 Control Register File	1074
15.44 Addressing Mode Register (AMR)	1075
15.44.1 Addressing Modes	1076
15.45 Syntax for Load/Store Address Generation	1076
15.45.1 Linear Addressing Mode	1077
15.46 Programming the T.I. DSP	1078
15.47 A Simple C Program	1079
15.48 The Generated Assembly Code	1080
15.48.1 Calling an Assembly Language Function	1083
15.49 Fibonacci Series in C Calling Assembly-Language Function	1087
15.50 Finite Impulse Response (FIR) Filter	1087
15.51 Infinite Impulse Response (IIR) Filter on the DSP	1088
15.52 Real-Time DSP Applications Using MATLAB-Simulink	1092
15.53 Detailed Steps for DSP Programming in C++ and Simulink	1094
15.53.1 Steps to Implement a C++ Program on the DSP Card	1094
15.53.2 Steps to Implement a Simulink Program on the DSP Card	1096
15.54 Problems	1098
15.55 Answers to Selected Problems	1101
16 Random Signal Processing	1105
16.1 Nonparametric Methods of Power Spectrum Estimation	1108
16.2 Correlation of Continuous-Time Random Signals	1109
16.3 Passage through an LTI System	1110
16.4 Wiener Filtering in Continuous-Time Domain	1113
16.5 Causal Wiener Filter	1116
16.6 Random Sequences	1118
16.7 From Statistical to Time Averages	1119
16.8 Correlation and Covariance in z -Domain	1120
16.9 Random Signal Passage through an LTI System	1121
16.10 PSD Estimation of Discrete-Time Random Sequences	1124
16.11 Fast Fourier Transform (FFT) Evaluation of the Periodogram	1128
16.12 Parametric Methods for PSD Estimation	1131
16.13 The Yule-Walker Equations	1132
16.14 System Modeling for Linear Prediction, Adaptive Filtering and Spectrum Estimation	1134
16.15 Wiener and Least-Squares Models	1134
16.16 Wiener Filtering	1135

16.17 Least-Squares Filtering	1138
16.18 Forward Linear Prediction	1138
16.19 Backward Linear Prediction	1140
16.20 Lattice MA FIR Filter Realization	1143
16.21 AR Lattice of Order p	1146
16.22 ARMA(p, q) Process	1146
16.23 Power Spectrum Estimation	1147
16.24 FIR Wiener Filtering of Noisy Signals	1148
16.25 Two-Sided IIR Wiener Filtering	1151
16.26 Causal IIR Wiener Filter	1152
16.27 Wavelet Transform	1154
16.28 Discrete Wavelet Transform	1157
16.29 Important Signal Processing MATLAB Functions	1164
16.30 lpc	1167
16.31 Yulewalk	1168
16.32 dfilt	1169
16.33 logspace	1170
16.34 FIR Filter Design	1170
16.35 fir2	1173
16.36 Power Spectrum Estimation Using MATLAB	1174
16.37 Parametric Modeling Functions	1174
16.38 prony	1175
16.39 Problems	1176
16.40 Answers to Selected Problems	1179

17 Distributions	1181
17.1 Introduction	1181
17.2 Distributions as Generalizations of Functions	1181
17.3 What is a Distribution?	1182
17.4 The Impulse as the Limit of a Sequence	1184
17.5 Properties of Distributions	1184
17.5.1 Linearity	1184
17.5.2 Time Shift	1185
17.5.3 Time Scaling	1185
17.5.4 Product with an Ordinary Function	1186
17.5.5 Symmetry	1186
17.5.6 Differentiation	1187
17.5.7 Multiplication Times an Ordinary Function	1187
17.5.8 Sequence of Distributions	1187
17.6 Approximating the Impulse	1187
17.7 Other Approximating Sequences and Functions of the Impulse	1190
17.8 Test Functions	1191
17.9 Convolution	1192
17.10 Multiplication by an Impulse Derivative	1193
17.11 The Dirac-Delta Impulse as a Limit of a Gaussian Function	1195
17.12 Fourier Transform of Unity	1196
17.13 The Impulse of a Function	1196
17.14 Multiplication by t	1199
17.15 Time Scaling	1199
17.16 Some Properties of the Dirac-Delta Impulse	1200
17.17 Additional Fourier Transforms	1201

17.18 Riemann–Lebesgue Lemma	1201
17.19 Generalized Limits	1202
17.20 Fourier Transform of Higher Impulse Derivatives	1204
17.21 The Distribution t^{-k}	1204
17.22 Initial Derivatives of the Transform	1206
17.23 The Unit Step Function as a Limit	1207
17.24 Inverse Fourier Transform and Gibbs Phenomenon	1208
17.25 Ripple Elimination	1212
17.26 Transforms of $ t $ and $tu(t)$	1213
17.27 The Impulse Train as a Limit	1214
17.28 Sequence of Distributions	1216
17.29 Poisson’s Summation Formula	1218
17.30 Moving Average	1219
17.31 Problems	1220
17.32 Answers to Selected Problems	1222
18 Generalization of Distributions Theory, Extending Laplace-, z- and Fourier-Related Transforms	1225
18.1 Introduction	1225
18.2 An Anomaly	1225
18.3 Generalized Distributions for Continuous-Time Functions	1226
18.3.1 Properties of Generalized Distributions in s Domain	1226
18.3.2 Linearity	1226
18.3.3 Shift in s	1226
18.3.4 Scaling	1227
18.3.5 Convolution	1227
18.3.6 Differentiation	1227
18.3.7 Multiplication of Derivative by an Ordinary Function	1228
18.4 Properties of the Generalized Impulse in s Domain	1228
18.4.1 Shifted Generalized Impulse	1228
18.4.2 Differentiation	1228
18.4.3 Convolution	1228
18.4.4 Convolution with an Ordinary Function	1229
18.4.5 Multiplication of an Impulse Times an Ordinary Function	1230
18.4.6 Multiplication by Higher Derivatives of the Impulse	1230
18.5 Additional Generalized Impulse Properties	1230
18.6 Generalized Impulse as a Limit of a Three-Dimensional Sequence	1232
18.7 Discrete-Time Domain	1234
18.8 3-D Test Function as a Possible Generalization	1235
18.8.1 Properties of Generalized Distributions in z -Domain	1235
18.8.2 Linearity	1236
18.8.3 Scaling in z -Domain	1236
18.8.4 Differentiation	1236
18.8.5 Convolution	1237
18.9 Properties of the Generalized Impulse in z -Domain	1237
18.9.1 Differentiation	1237
18.10 Generalized Impulse as Limit of a 3-D Sequence	1238
18.10.1 Convolution of Generalized Impulses	1240
18.10.2 Convolution with an Ordinary Function	1241
18.11 Extended Laplace and z -Transforms	1242
18.12 Generalization of Fourier-, Laplace- and z -Related Transforms	1242

18.13 Hilbert Transform Generalization	1245
18.14 Generalizing the Discrete Hilbert Transform	1247
18.15 Generalized Hartley Transform	1247
18.16 Generalized Discrete Hartley Transform	1248
18.17 Generalization of the Mellin Transform	1249
18.18 Multidimensional Signals and the Solution of Differential Equations	1251
18.19 Problems	1254
18.20 Answers to Selected Problems	1255
A Appendix	1257
A.1 Symbols	1257
A.2 Frequently Needed Expansions	1257
A.3 Important Trigonometric Relations	1259
A.4 Orthogonality Relations	1259
A.5 Frequently Encountered Functions	1260
A.6 Mathematical Formulae	1260
A.7 Frequently Encountered Series Sums	1261
A.8 Biographies of Pioneering Scientists	1262
A.9 Plato (428 BC–347 BC)	1262
A.10 Ptolemy (circa 90–168 AD)	1264
A.11 Euclid (circa 300 BC)	1265
A.12 Abu Ja'far Muhammad ibn Musa Al-Khwarizmi (780–850 AD)	1266
A.13 Nicolaus Copernicus (1473–1543)	1269
A.14 Galileo Galilei (1564–1642)	1272
A.15 Sir Isaac Newton (1643–1727)	1274
A.16 Guillaume-François-Antoine de L'Hôpital (1661–1704)	1278
A.17 Pierre-Simon Laplace (1749–1827)	1279
A.18 Gaspard Clair François Marie, Baron Riche de Prony (1755–1839)	1281
A.19 Jean Baptiste Joseph Fourier (1768–1830)	1285
A.20 Johann Carl Friedrich Gauss (1777–1855)	1289
A.21 Friedrich Wilhelm Bessel (1784–1846)	1290
A.22 Augustin-Louis Cauchy (1789–1857)	1292
A.23 Niels Henrik Abel (1802–1829)	1295
A.24 Johann Peter Gustav Lejeune Dirichlet (1805–1859)	1297
A.25 Pafnuty Lvovich Chebyshev (1821–1894)	1298
A.26 Paul A.M. Dirac	1300
References	1303
Index	1307