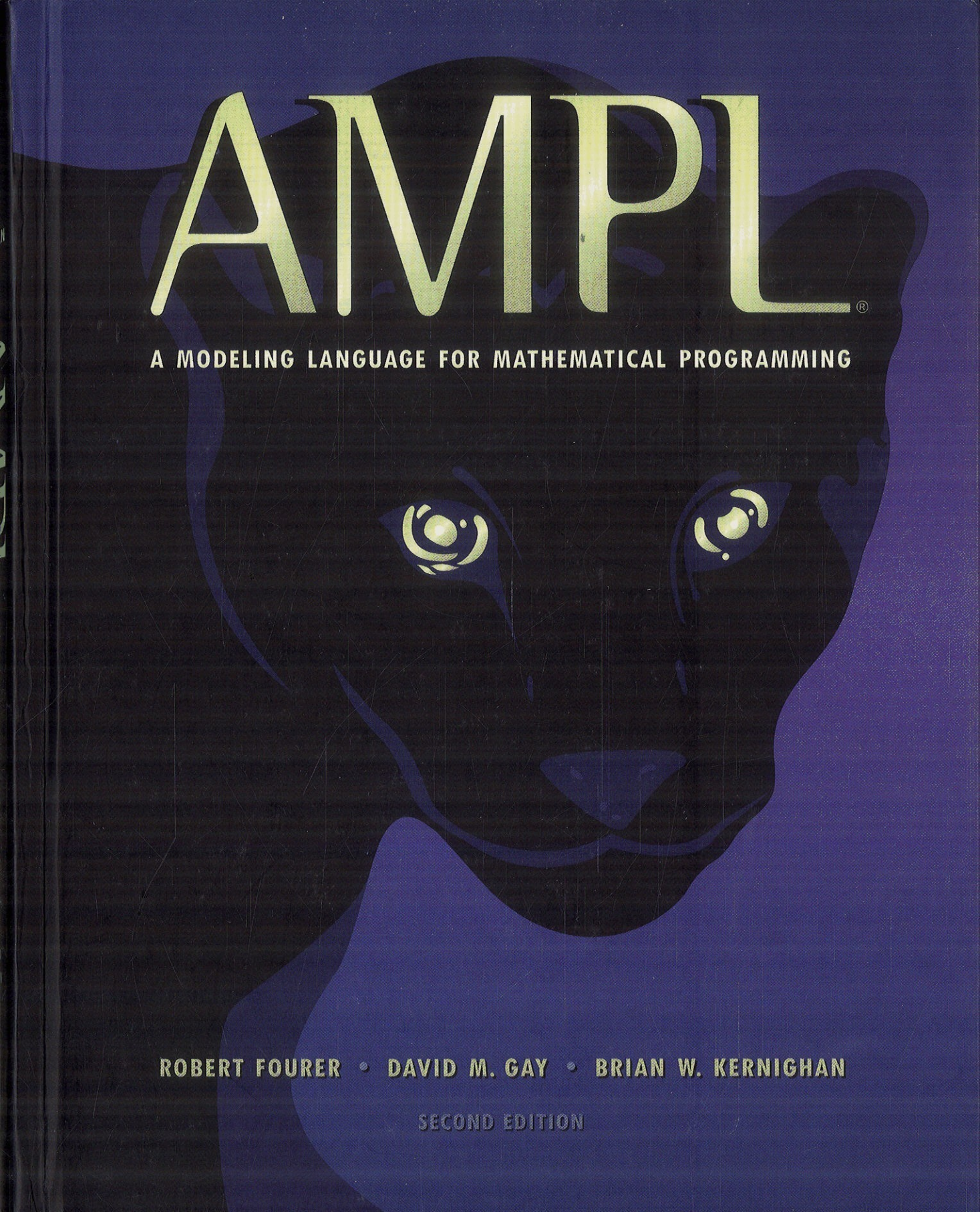


AMPL[®]



A MODELING LANGUAGE FOR MATHEMATICAL PROGRAMMING

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SECOND EDITION

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