

supersymmetry

DeMYSTiFieD

A SELF-TEACHING GUIDE



Covers supercharges, SUPERFIELDS, superspace, SUSY breaking, the minimal supersymmetric standard model, and more



LOADED with DETAILED examples, ILLUSTRATIONS, and explanations



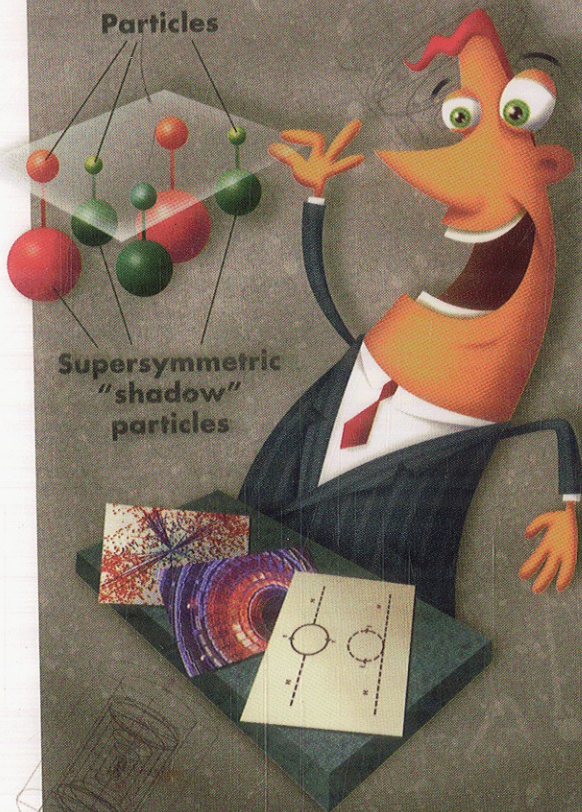
Perfect for SELF-STUDY or as a classroom SUPPLEMENT



COMPLETE with end-of-chapter QUIZZES and a final EXAM

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CONTENTS



Acknowledgments xiii

CHAPTER 1

Introduction 1

- 1.1 What Is Supersymmetry, and Why Is It Exciting (the Short Version)? 1
- 1.2 What This Book Is and What It Is Not 3
- 1.3 Effective Field Theories, Naturalness, and the Higgs Mass 6
- 1.4 Further Reading 11

CHAPTER 2

A Crash Course on Weyl Spinors 13

- 2.1 Brief Review of the Dirac Equation and of Some Matrix Properties 14
- 2.2 Weyl versus Dirac Spinors 17
- 2.3 Helicity 22
- 2.4 Lorentz Transformations and Invariants 24
- 2.5 A First Notational Hurdle 26
- 2.6 Building More Lorentz Invariants Out of Weyl Spinors 28
- 2.7 Invariants Containing Lorentz Indices 32
- 2.8 A Useful Identity 33
- 2.9 Introducing a New Notation 34
- 2.10 Quiz 40

CHAPTER 3	New Notation for the Components of Weyl Spinors	43
	3.1 Building Lorentz Invariants	51
	3.2 Index-Free Notation	53
	3.3 Invariants Built Out of Two Left-Chiral Spinors	56
	3.4 The ϵ Notation for $\pm i\sigma^2$	57
	3.5 Notation for the Indices of σ^μ and $\bar{\sigma}^\mu$	60
	3.6 Quiz	65
CHAPTER 4	The Physics of Weyl, Majorana, and Dirac Spinors	67
	4.1 Charge Conjugation and Antiparticles for Dirac Spinors	68
	4.2 CPT Invariance	70
	4.3 A Massless Weyl Spinor	72
	4.4 Adding a Mass: General Considerations	73
	4.5 Adding a Mass: Dirac Spinors	74
	4.6 The QED Lagrangian in Terms of Weyl Spinors	76
	4.7 Adding a Mass: Majorana Spinors	78
	4.8 Dirac Spinors and Parity	81
	4.9 Definition of the Masses of Scalars and Spinor Fields	82
	4.10 Adding a Mass: Weyl Spinor	85
	4.11 Relation Between Weyl Spinors and Majorana Spinors	86
	4.12 Quiz	88
CHAPTER 5	Building the Simplest Supersymmetric Lagrangian	89
	5.1 Dimensional Analysis	90
	5.2 The Transformation of the Fields	91
	5.3 Transformation of the Lagrangian	95
	5.4 Quiz	99

CHAPTER 6	The Supersymmetric Charges and Their Algebra	101
	6.1 Charges: General Discussion	102
	6.2 Explicit Representations of the Charges and the Charge Algebra	107
	6.3 Finding the Algebra Without the Explicit Charges	111
	6.4 Example	113
	6.5 The SUSY Algebra	115
	6.6 Nonclosure of the Algebra for the Spinor Field	125
	6.7 Introduction of an Auxiliary Field	128
	6.8 Closure of the Algebra	131
	6.9 Quiz	131
CHAPTER 7	Applications of the SUSY Algebra	133
	7.1 Classification of States Using the Algebra: Review of the Poincaré Group	134
	7.2 Effects of the Supercharges on States	140
	7.3 The Massless SUSY Multiplets	144
	7.4 Massless SUSY Multiplets and the MSSM	146
	7.5 Two More Important Results	147
	7.6 The Algebra in Majorana Form	150
	7.7 Obtaining the Charges from Symmetry Currents	151
	7.8 Explicit Supercharges as Quantum Field Operators	153
	7.9 The Coleman-Mandula No-Go Theorem	156
	7.10 The Haag-Lopuszanski-Sohnius Theorem and Extended SUSY	157
	7.11 Quiz	158
CHAPTER 8	Adding Interactions: The Wess-Zumino Model	159
	8.1 A Supersymmetric Lagrangian With Masses and Interactions	160
	8.2 A More General Lagrangian	167

	8.3	The Full Wess-Zumino Lagrangian	173
	8.4	The Wess-Zumino Lagrangian in Majorana Form	175
	8.5	Quiz	176
CHAPTER 9		Some Explicit Calculations	177
	9.1	Refresher About Calculations of Processes in Quantum Field Theory	178
	9.2	Propagators	182
	9.3	One Point Function	185
	9.4	Propagator of the B Field to One Loop	189
	9.5	Putting It All Together	201
	9.6	A Note on Nonrenormalization Theorems	203
	9.7	Quiz	204
CHAPTER 10		Supersymmetric Gauge Theories	205
	10.1	Free Supersymmetric Abelian Gauge Theory	206
	10.2	Introduction of the Auxiliary Field	209
	10.3	Review of Nonabelian Gauge Theories	211
	10.4	The QCD Lagrangian in Terms of Weyl Spinors	217
	10.5	Free Supersymmetric Nonabelian Gauge Theories	219
	10.6	Combining an Abelian Vector Multiplet With a Chiral Multiplet	222
	10.7	Eliminating the Auxiliary Fields	232
	10.8	Combining a Nonabelian Gauge Multiplet With a Chiral Multiplet	233
	10.9	Quiz	237
CHAPTER 11		Superspace Formalism	239
	11.1	The Superspace Coordinates	240
	11.2	Example of Spacetime Translations	242

	11.3	Supersymmetric Transformations of the Superspace Coordinates	244
	11.4	Introduction to Superfields	248
	11.5	Aside on Grassmann Calculus	250
	11.6	The SUSY Charges as Differential Operators	255
	11.7	Constraints and Superfields	261
	11.8	Quiz	268
CHAPTER 12		Left-Chiral Superfields	269
	12.1	General Expansion of Left-Chiral Superfields	269
	12.2	SUSY Transformations of the Component Fields	273
	12.3	Constructing SUSY Invariants Out of Left-Chiral Superfields	277
	12.4	Relation Between the Superpotential in Terms of Superfields and the Superpotential of Chapter 8	285
	12.5	The Free Part of the Wess-Zumino Model	288
	12.6	Why Does It All Work?	292
	12.7	Quiz	295
CHAPTER 13		Supersymmetric Gauge Field Theories in the Superfield Approach	297
	13.1	Abelian Gauge Invariance in the Superfield Formalism	297
	13.2	Explicit Interactions Between a Left-Chiral Multiplet and the Abelian Gauge Multiplet	303
	13.3	Lagrangian of a Free Supersymmetric Abelian Gauge Theory in Superfield Notation	306
	13.4	The Abelian Field-Strength Superfield in Terms of Component Fields	308
	13.5	The Free Abelian Supersymmetric Lagrangian from the Superfield Approach	313
	13.6	Supersymmetric QED	317
	13.7	Supersymmetric Nonabelian Gauge Theories	322
	13.8	Quiz	324

CHAPTER 14	SUSY Breaking	325
	14.1 Spontaneous Supersymmetry Breaking	326
	14.2 F-Type SUSY Breaking	330
	14.3 The O’Raifeartaigh Model	331
	14.4 Mass Spectrum: General Considerations	334
	14.5 Mass Spectrum of the O’Raifeartaigh Model for $m^2 \geq 2g^2 M^2$	335
	14.6 The Supertrace	339
	14.7 D-Type SUSY Breaking	340
	14.8 Second Example of D-Type SUSY Breaking	343
	14.9 Explicit SUSY Breaking	344
	14.10 Quiz	350
CHAPTER 15	Introduction to the Minimal Supersymmetric Standard Model	351
	15.1 Lightning Review of the Standard Model	351
	15.2 Spontaneous Symmetry Breaking in the Standard Model	360
	15.3 Aside on Notation	364
	15.4 The Left-Chiral Superfields of the MSSM	365
	15.5 The Gauge Vector Superfields	368
	15.6 The MSSM Lagrangian	368
	15.7 The Superpotential of the MSSM	371
	15.8 The General MSSM Superpotential	377
	15.9 Quiz	378
CHAPTER 16	Some Phenomenological Implications of the MSSM	379
	16.1 Supersymmetry Breaking in the MSSM	380
	16.2 The Scalar Potential, Electroweak Symmetry Breaking, and All That	381
	16.3 Finding a Minimum	384
	16.4 The Masses of the Gauge Bosons	387
	16.5 Masses of the Higgs	392

16.6	Masses of the Leptons, Quarks, and Their Superpartners	399
16.7	Some Other Consequences of the MSSM	400
16.8	Coupling Unification in Supersymmetric GUT	401
16.9	Quiz	412
	Final Exam	413
	References	417
APPENDIX A	Useful Identities	421
APPENDIX B	Solutions to Exercises	427
APPENDIX C	Solutions to Quizzes	461
APPENDIX D	Solutions to Final Exam	469
	Index	475