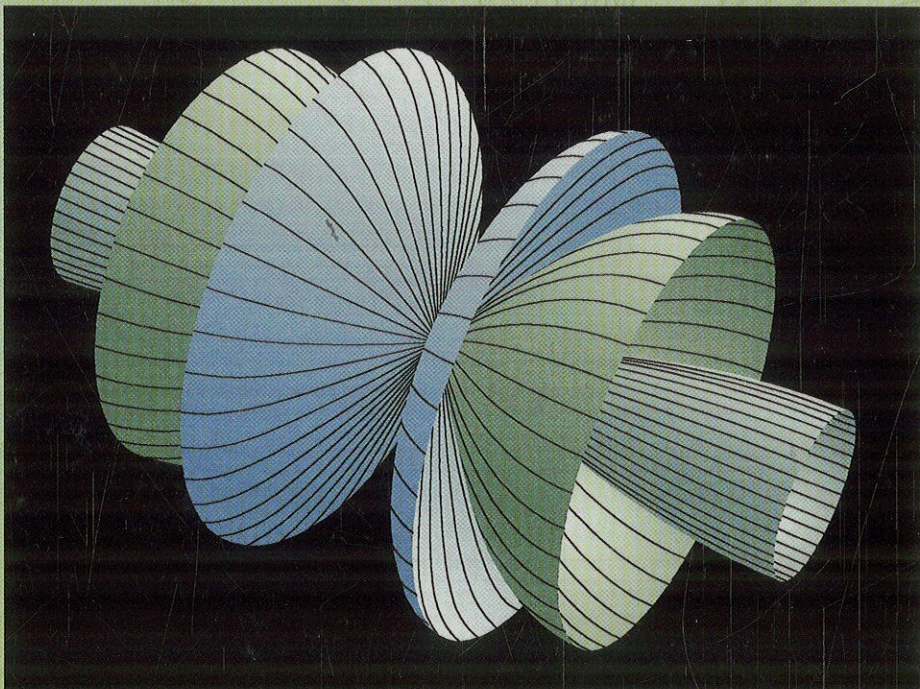


Second Edition

A First Course in
**STRING
THEORY**



Barton Zwiebach

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