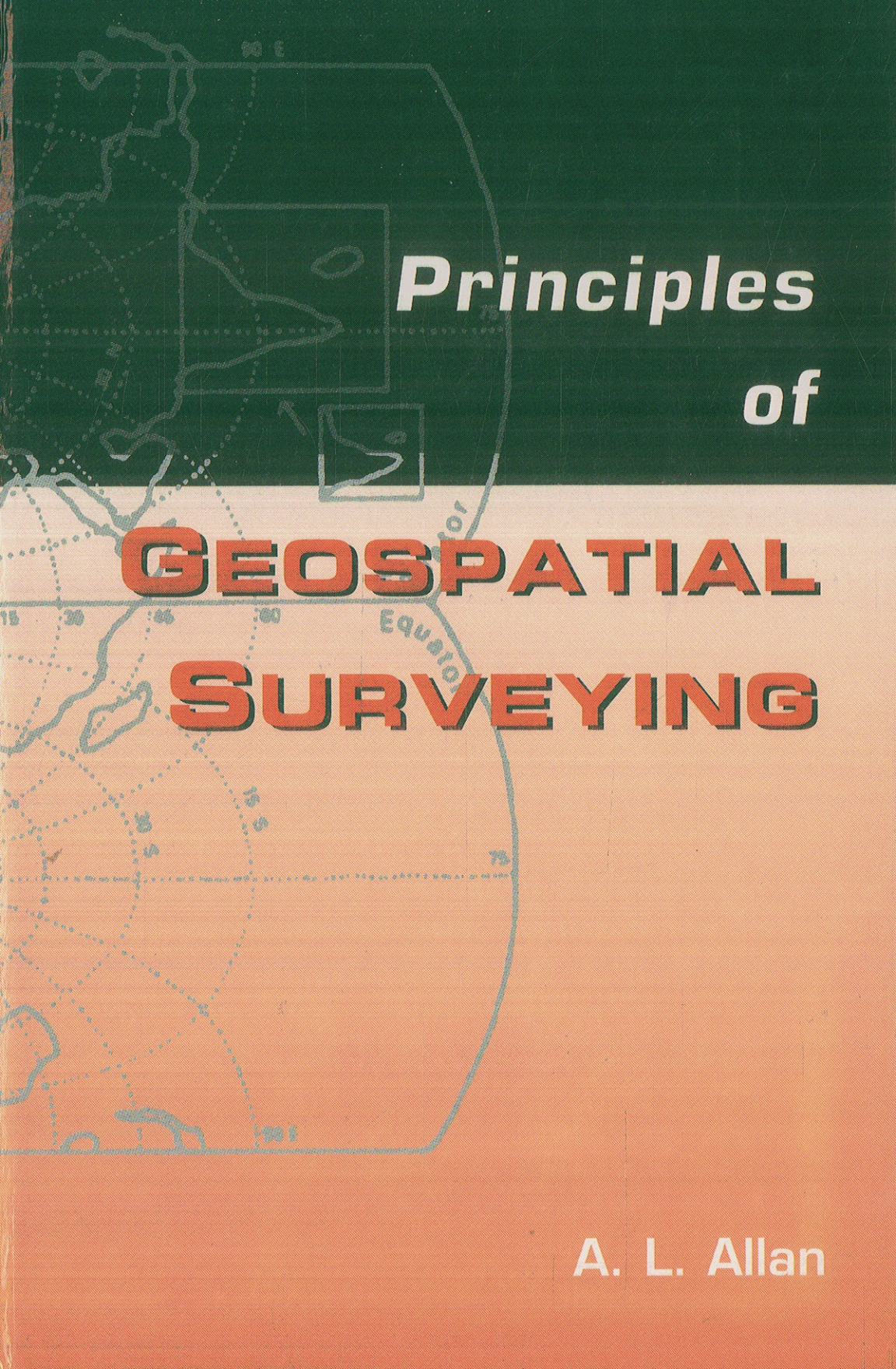




Principles
of

**GEOSPATIAL
SURVEYING**

A. L. Allan

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