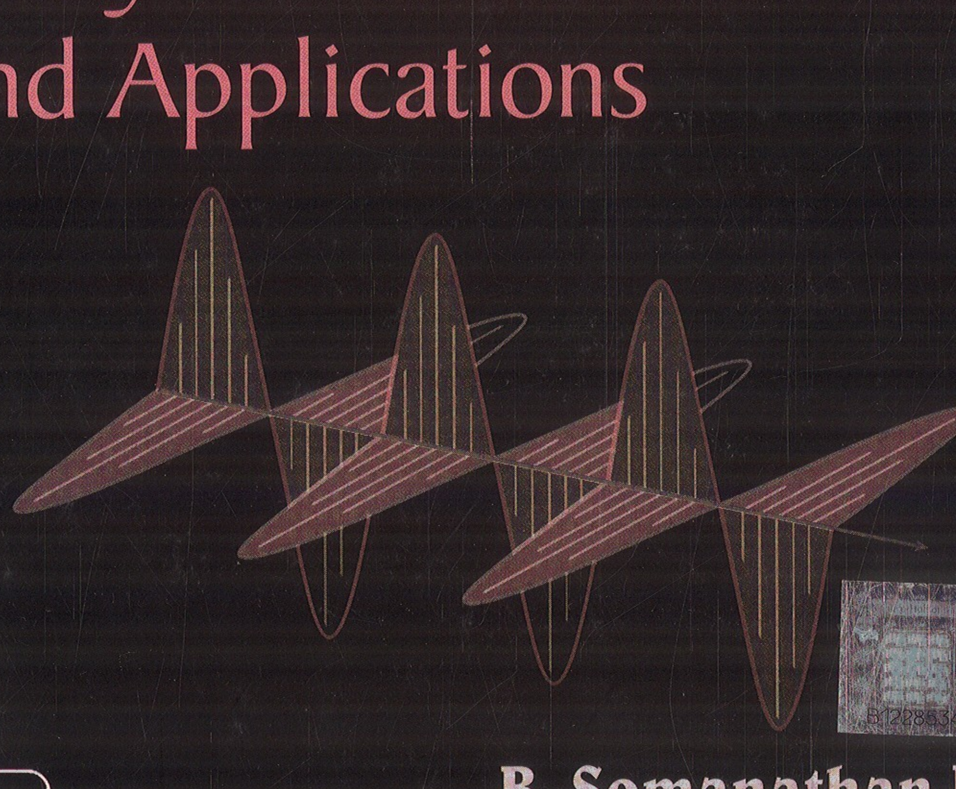
Eastern Economy Edition

APPLIED ELECTROMAGNETIC THEORY

Analyses, Problems and Applications



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