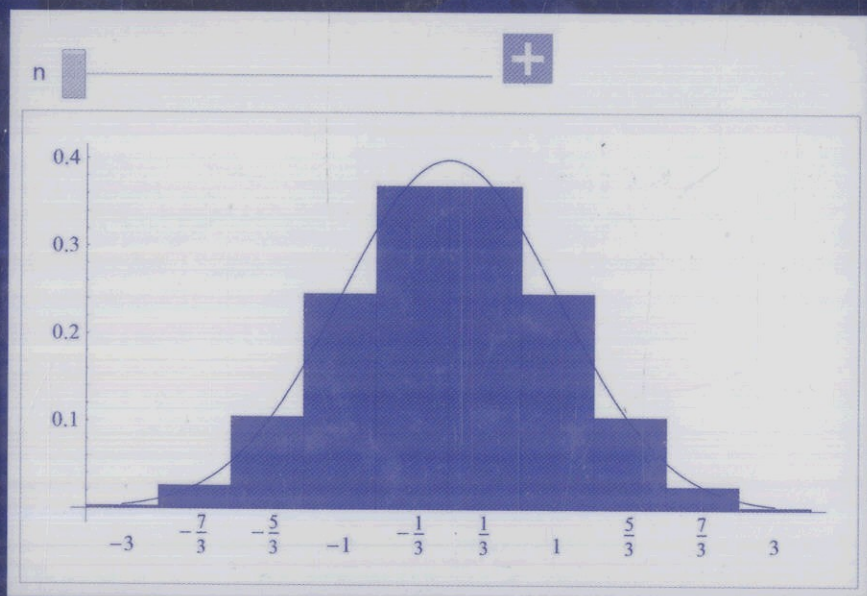


TEXTBOOKS in MATHEMATICS

INTRODUCTION TO
Probability with
Mathematica[®]
Second Edition



Kevin J. Hastings



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A CHAPMAN & HALL BOOK

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