

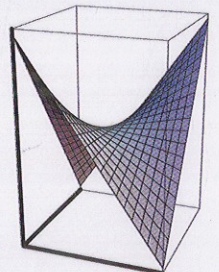
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Computational Optimal Control

Tools and Practice



 WILEY



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