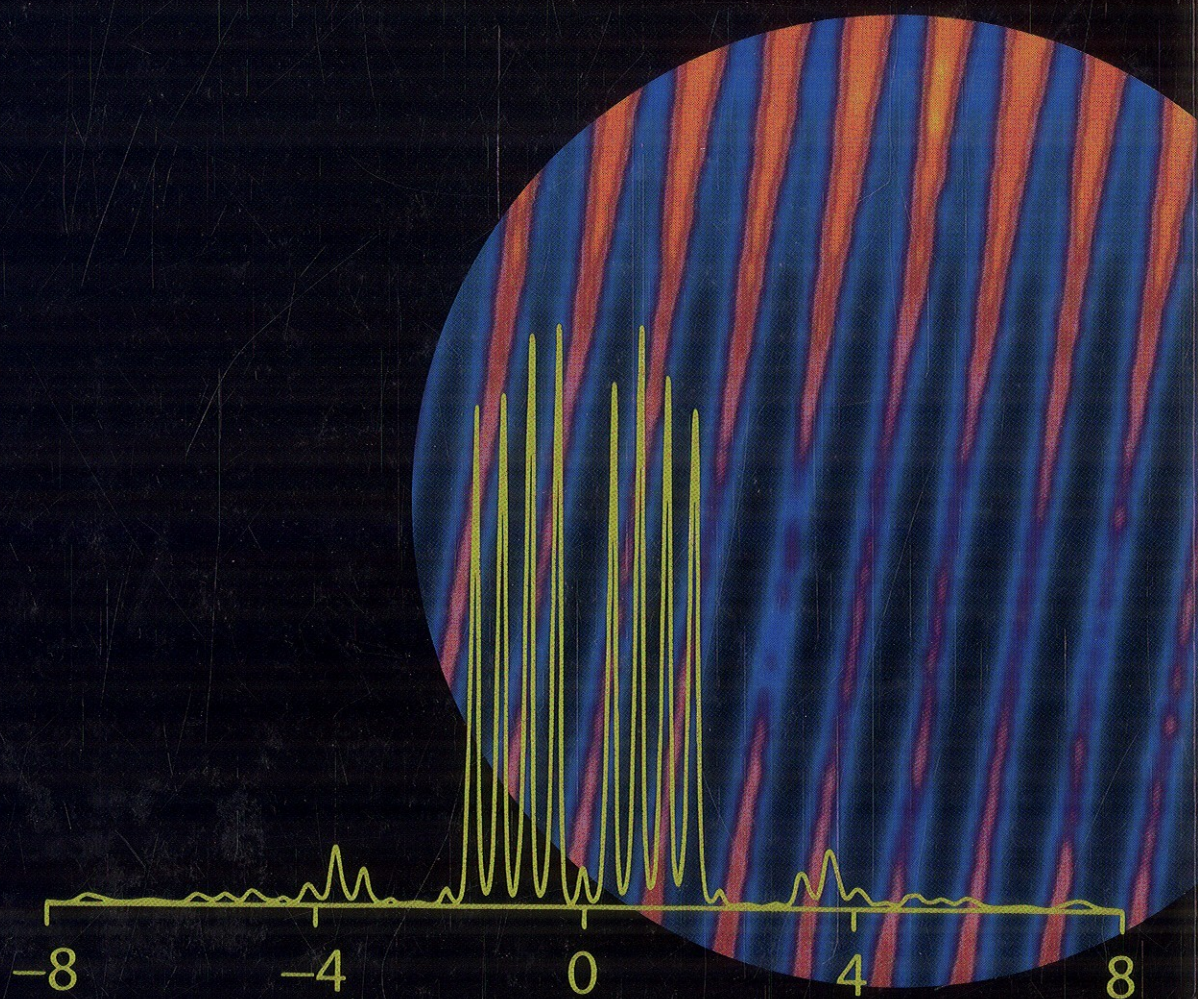


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# Ultrafast Optics

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 **WILEY**

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