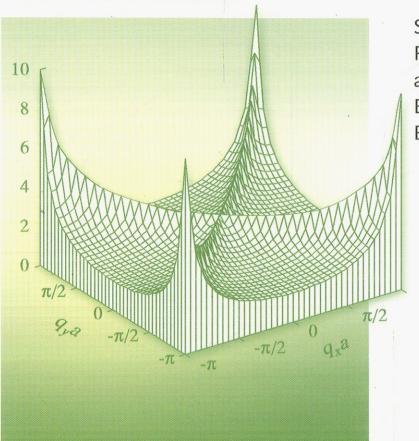
László Mihály and Michael C. Martin



Solid State Physics

Problems and Solutions



Second, Revised and Enlarged Edition

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