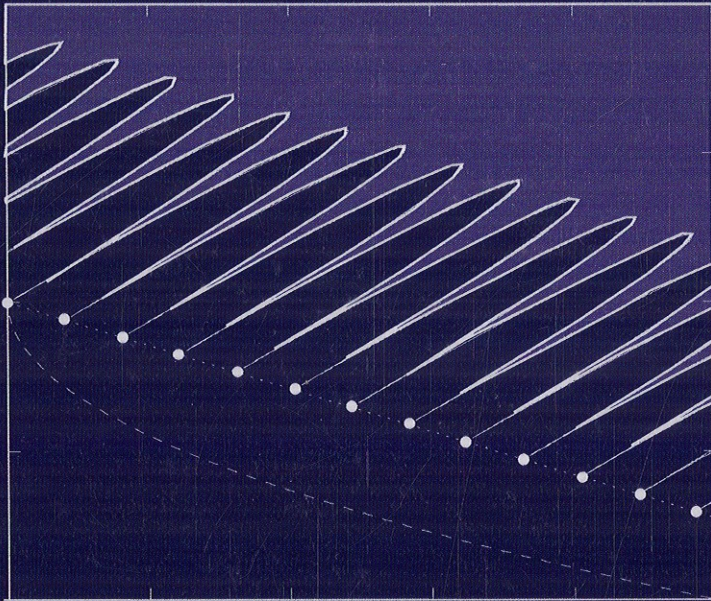


 WILEY

Multi-Objective Optimization using Evolutionary Algorithms



KALYANMOY DEB

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