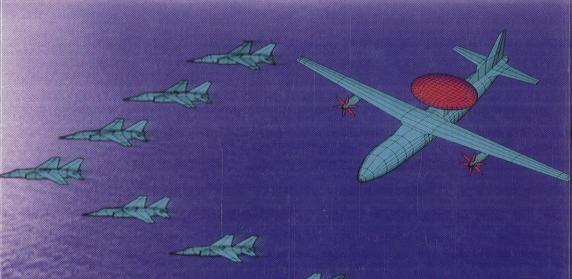
## PARALLEL SOLUTION OF INTEGRAL EQUATION-BASED EM PROBLEMS IN THE FREQUENCY DOMAIN



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## **Contents**

Preface				•		•	•						xiii
Acknowle	edgm	ents	•	•	٠	•	•	•	•	•			xvii
Acronym	S			•	•	•	•	•			•	•	xix
Chapter	1	Inti	rodu	ction			•			•			1
	1.0	Sun	nmar	у.			٠						1
	1.1				w of	f Para	llel C	EΜ					1
		1.1.	1 Co	mput	atior	ıal Ele	ectron	nagne	etics				1
						nputat				igneti	cs.		3
	1.2					ns Ac							9
	1.3					Emple					tions		12
						X — S						ckage	13
						— Par							16
	1.4	Cor	ıclus	ion	١,							٠.	19
		Ref	eren	ces						•			19
Chantar	2	In t	Core	and	Ont	-of-C	oro T	II <b>V</b> o	etari	zation	for		
Chapter	2					Equa				,			27
	2.0	Sur	nmar	<b>*\$</b> .7									27
	2.1					· rom a		A.Cod	ام	•	•	•	28
	2.2					x Equ				•	•	•	28
	2.3					ntation				Olver		•	32
	2.5					ution					•	•	32
						K: Tw					-Cvcl	ic.	
		. ر. ب				ibutic						10	36
		23				Physi		-		rix D	vistrib	otion	38
						ution					IDUA IO	441011	50
		2.5				K and				*********			40
	2.4	Dat				ion for				Solv	rer		42
	2.5					actor					VI .	•	43
	د.ب					of Se					nd .	•	-13
		۷.۶				g Out							45
						ght-Le					1110	•	45
				5.1.2		gm-Lo eft-Loc					•	•	47
			۷,,		200	g. Doc	8	111501	0010116	•	•	•	. ,

		2.5.2 Implementation of the Serial Left-Looking	
		Out-of-Core LU Algorithm	50
		2.5.3 Design of a One-Slab Left-Looking Out-of-Core	
		LU Algorithm	55
	2.6	Parallel Implementation of an Out-of-Core LU	
		Algorithm	61
		2.6.1 Parallel Implementation of an Out-of-Core	
		LU Algorithm Using ScaLAPACK	61
		2.6.2 Parallel Implementation of an Out-of-Core	
		LU Algorithm Using PLAPACK	64
		2.6.3 Overlapping of the I/O with the Computation .	65
		2.6.4 Checkpointing in an Out-of-Core Solver	65
	2.7	Solving a Matrix Equation Using the Out-of-Core LU	
		Matrices	66
	2.8	Conclusion	69
		References	69
G)	•	A B CONTROL OF A STATE	_
Chapter	3	A Parallel MoM Code Using RWG Basis Functions an	d
		ScaLAPACK-Based In-Core and	
		Out-of-Core Solvers	71
	3.0	Summary	71
	3.1	Electric Field Integral Equation (EFIE)	71
	3.2	Use of the Piecewise Triangular Patch (RWG) Basis	
		Functions	74
	3.3	Functions	76
	3.4	Matrix Equation for MoM	78
	3.5	Calculation of the Various Integrals	79
		3.5.1 Evaluation of the Fundamental Integrals	79
		3.5.2 Extraction of the Singularity	80
	3.6	Calculation of the Fields	81
	3.7	Parallel Matrix Filling — In-Core Algorithm	81
	3.8	Parallel Matrix Filling — Out-of-Core Algorithm .	86
	3.9	Numerical Results from a Parallel In-Core MoM Solver	88
		3.9.1 Numerical Results Compared with other Methods	88
		3.9.1.1 A PEC Cube	88
		3.9.1.2 A Combined Cube-and-Sphere PEC Model	88
		3.9.2 Different Metrics Used to Assess the Degree	
		of Parallel Efficiency	88
		3.9.3 Efficiency and Portability of a Parallel MoM	
		In-Core Solver	92
	3.10	Numerical Results from a Parallel Out-of-Core MoM	
		Solver	96
		3.10.1 Parallel Out-of-Core Solver Can Be as Efficient as	
		a Parallel In-Core Solver.	96

		3.10.2 Scalability and Portability of the Parallel	0.0
		Out-of-Core Solver	98
	3.11	Conclusion	104
		References	105
Chapter	4	A Parallel MoM Code Using Higher-Order Basis Functions and ScaLAPACK-Based In-Core	
		and Out-of-Core Solvers	107
	4.0	Summary	107
	4.1	Formulation of the Integral Equation for Analysis of	107
	4.0	Dielectric Structures	107
	4.2	A General Formulation for the Analysis of Composite	110
		Metallic and Dielectric Structures	110
	4.3	Geometric Modeling of the Structures	114
		4.3.1 Right-Truncated Cone to Model Wire Structures 4.3.2 Bilinear Surface for Modeling Arbitrarily Shaped	114
		Surfaces	116
	4.4	Higher-Order Basis Functions	117
	₹.⊤	4.4.1 Current Expansion along a Thin PEC Wire	117
		4.4.2 Current Expansion over a Bilinear Surface	119
	4.5	Testing Procedure	124
	110	4.5.1 Testing Procedure for Thin PEC Wires	124
		4.5.2 Testing Procedure for Bilinear Surfaces	128
	4.6	Parallel In-Core and Out-of-Core Matrix Filling Schemes	
	1.0	4.6.1 Parallel In-Core Matrix Filling Scheme	132
		4.6.2 Parallel Out-of-Core Matrix Filling Scheme .	134
	4.7	Numerical Results Computed on Different Platforms.	136
	•••	4.7.1 Performance Analysis for the Parallel	120
		In-Core Integral Equation Solver	136
		4.7.1.1 Comparison of Numerical Results Obtained	
		on Single-Core and Multicore Platforms	136
		4.7.1.2 Numerical Results Obtained on Single-Core	
		Platforms	141
		4.7.1.2.1 Radiation from a Vivaldi	
		Antenna Array	141
		4.7.1.2.2 Scattering from a Full-Size	
		Airplane	144
		4.7.1.3 Numerical Results Obtained on	
		Multicore Platforms	146
		4.7.2 Performance Analysis for the Parallel Out-of-Core	
		Integral Equation Solver	147
		4.7.2.1 Vivaldi Antenna Array — a Large Problem	,
		Solved on Small Computer Platforms .	147

		4.7.2.2 S									!
						ver C		e as $E$	fficiei	nt as	
					el In-C		٠,		. ~		149
		4.7.2.3 \$	Soluti	on fo	r a Fi	ıll-Siz	e Air,	plane	— Sc	calabii	'ity
					oility e	of the	Para	ilei O	ut-of-	Core	
			Solve		,				•		150
		4.7.2.4 S									
			_		biem i	Solve	d on I	Vine I	vodes	of	1.50
	10		CEM-	-4.	•	٠	•	•	•	•	153
	4.8	Conclusion References	•		•	•		•	•	•	155
		References	•	•	•	•		•	•	•	155
Chapter	5	Tuning the P	erfor	man	ce of	a Par	allel	Integ	ral		
Chapter	•	Equation Sol		•					- 441		157
		Equation So.	• • • •	•	•	•	•	•	•	•	10,
	5.0	Summary.									157
	5.1	Anatomy of a	Parai	llel O	ut-of	-Core	Integ	ral			
		Equation Solv									157
		5.1.1 Various	Com	pone	nts of	a Par	allel				
		Out-of-C	Core S	Solve	r that	Can I	Be Ol	oserve	ed thr	ough	
		Ganglia	and 7	Γuneo	i .						158
		5.1.2 CPU Tir	nes o	f Par	allel I	n-Co	re and	l Out-	of-Co	ore	
		Integral	Equa	tion S	Solve	rs.					161
		5.1.3 Perform	ance	of a (	Code	Varie	s with	the A	4mou	ınt	
		of Stora	ge Us	sed or	n the l	Hard :	Disk				165
	5.2	Block Size									170
	5.3	Shape of the I									173
	5.4	Size of the In-									176
		5.4.1 Optimiz							Code		
		Using H									177
		5.4.1.1									177
			5.4.1.			ew of			with		
						ent IA					177
			5.4.1.			s on M		Filli	ng an	d	
			~			Solvi		D.41.6		•	181
		5.4.1.2									188
		5.4.2 Optimiz							Code		100
		Using R						D (		•	190
	E	5.4.3 Influence									194
	5.5	Relationship l			nape o	or the	Proc	ess G	rid an	α	107
	5 4	In-Core Buffe Overall Perform			o Don	allal (	Trat ==	e C	. C = 1		197
	5.6	HPC Clusters			a rar	anei (	Jul-0	ı-Cor	5017	er on	201
	5.7	Conclusion		•	•	•	•	•	•	•	201
	5.1	References	•	•	•	•	•	•	•	•	205
		TOTOLOHOOS					•	•			200

Chapter	6	Refinement of the Solution Using the Iterative Conjugate Gradient Method	207
	6.0	Summary	207
	6.1	Development of the Conjugate Gradient Method	207
	6.2	The Iterative Solution of a Matrix Equation	212
	6.3	Parallel Implementation of the CG Algorithm	213
	6.4	A Parallel Combined LU-CG Scheme to Refine the	
		LU Solution	215
	6.5	Conclusion	216
		References	217
Chapter	7	A Parallel MoM Code Using Higher-Order Basis Functions and PLAPACK-Based In-Core and	
		Out-of-Core Solvers	219
	7.0	Summary	219
	7.1	Introduction	219
	7.2	Factors that Affect a Parallel In-Core and Out-of-Core	
		Matrix Filling Algorithm	220
	7.3	Numerical Results	224
		7.3.1 Radiation from an Array of Vivaldi Antennas .	224
		7.3.2 Scattering from an Electrically Large Aircraft .	228
		7.3.3 Discussion of the Computational FLOPS	
		Achieved	230
	7.4	Conclusion	231
		References	231
Chapter	8	Applications of the Parallel Frequency-Domain	
		Integral Equation Solver — TIDES	233
	8.0	Summary	233
	8.1	Performance Comparison between TIDES and a	
		Commercial EM Analysis Software	234
		8.1.1 Analysis of a Scattering Problem	234
		8.1.2 Analysis of a Radiation Problem	237
		8.1.3 Analysis of a Coupling Problem	241
	8.2	EMC Prediction for Multiple Antennas Mounted	
		on an Electrically Large Platform	243
	8.3	Analysis of Complex Composite Antenna Array .	248
	8.4	Array Calibration for Direction-of-Arrival Estimation	249
	8.5	Radar Cross Section (RCS) Calculation of Complex	
		Targets	252
		8.5.1 RCS Calculation of a Squadron of Tanks	252
		8.5.2 RCS of the Tanks inside a Forest Environment.	254

8.6	8.5.3 RCS from an Aircraft and a Formation of Aircraft 8.5.4 RCS Simulation with Million Level Unknowns. 8.5.5 RCS of an Aircraft Carrier Analysis of Radiation Patterns of Antennas Operating Inside a Radome Along with the Platform on								
	Which It Is Mounted	264							
8.7	Electromagnetic Interference (EMI) Analysis of a	204							
~~.	Communication System	268							
8.8	Comparison between Computations Using TIDES and								
	Measurement data for Complex Composite Structures.	271							
8.9	Conclusion	273							
	References	273							
Appendix A	A Summary of the Computer Platforms Used in This								
	Book	275							
A.(	•••••••••••••••••••••••••••••••••••••••	275							
A.1		275							
A.2		284							
	References	285							
	A								
Appendix B	An Efficient Cross-Platform Compilation of the	*0=							
Appendix B	An Efficient Cross-Platform Compilation of the ScaLAPACK and PLAPACK Routines	287							
•	ScaLAPACK and PLAPACK Routines								
В.(	ScaLAPACK and PLAPACK Routines	<b>287</b> 287							
•	ScaLAPACK and PLAPACK Routines	287							
B.0 B.1	ScaLAPACK and PLAPACK Routines	287 287							
В.(	ScaLAPACK and PLAPACK Routines	287 287 288							
B.0 B.1	ScaLAPACK and PLAPACK Routines	287 287 288 288							
B.0 B.1	ScaLAPACK and PLAPACK Routines	287 288 288 288							
B.0 B.1	ScaLAPACK and PLAPACK Routines	287 288 288 288 289							
B.0 B.1	ScaLAPACK and PLAPACK Routines	287 287 288 288 288 289 289							
B.0 B.1	ScaLAPACK and PLAPACK Routines	287 287 288 288 288 289 289 293							
B.0 B.1	ScaLAPACK and PLAPACK Routines	287 288 288 288 289 289 293 296							
B.0 B.1	ScaLAPACK and PLAPACK Routines	287 287 288 288 289 289 293 296 297							
B.0 B.1 B.2	ScaLAPACK and PLAPACK Routines	287 288 288 288 289 289 293 296 297 298							
B.0 B.1 B.2	ScaLAPACK and PLAPACK Routines	287 288 288 288 289 293 296 297 298 298							
B.0 B.1 B.2	ScaLAPACK and PLAPACK Routines	287 288 288 288 289 289 293 296 297 298							
B.0 B.1 B.2	ScaLAPACK and PLAPACK Routines	287 288 288 288 289 293 296 297 298 298 298							

Appendix	C	An Example of a Parallel MoM Source Code for Analysis of 2D EM Scattering										
		Allatysis of	ZD ENI S	cattern	ığ	•	•	•	•	303		
	C.0	Summary.								303		
	C.1	Introduction	of MoM				,			303		
	C.2	Solution of a	Two-Di	mension	al Sc	atterii	ng Pr	oblem		305		
		Solution of a Two-Dimensional Scattering Problem . C.2.1 Development of the Integral Equation and the										
			Solution		_					305		
		C.2.2 Evalua	tion of th							308		
	C.3	Implementat	ion of a S	Serial M	oM C	ode				309		
		C.3.1 Flowel					MoM	Code		309		
		C.3.2 A Seri								•		
			ring Prob							312		
	C.4	Implementat	_					·	į	313		
	· · ·	C.4.1 Flowel						M.Cod	le	313		
		C.4.2 A Para										
			2D Scat							318		
	C.5	Compilation							•	331		
	C.6	Conclusion	and LAC	Junon O.	Line	arati	CI CO	ac	•	333		
	C.0	References		•	•	•	•	•	•	333		
		References		•	•	•	•	•	•	333		
Index				•						335		