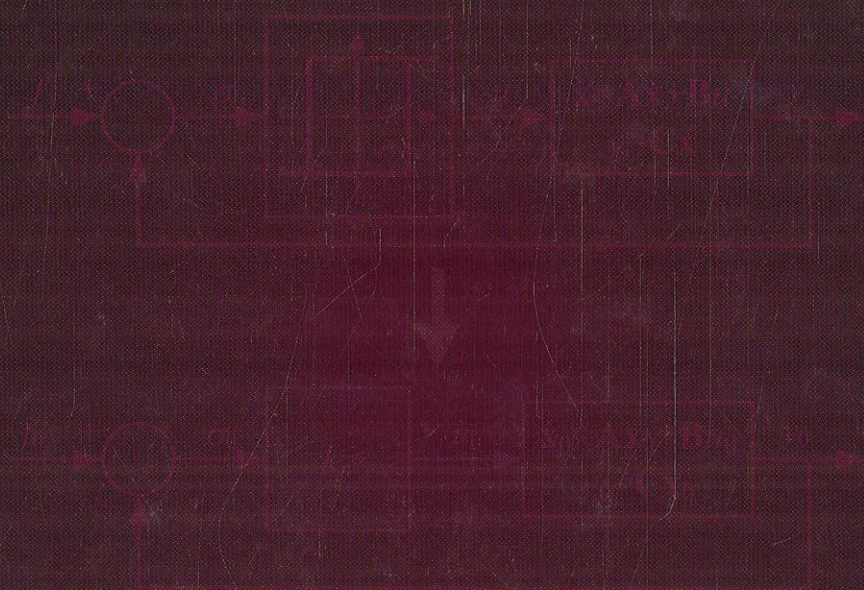


BIRKHAUSER

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Discontinuous Control Systems

Frequency-Domain
Analysis and Design



Contents

Preface	VII
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Part I The locus of a perturbed relay system theory

1 The servo problem in discontinuous control systems	3
1.1 Introduction	3
1.2 Fundamentals of frequency-domain analysis of periodic motions in nonlinear systems.....	5
1.3 Relay servo systems.....	10
1.4 Symmetric oscillations in relay servo systems: DF analysis	12
1.5 Asymmetric oscillations in relay servo systems: DF analysis ...	14
1.6 Slow signal propagation through a relay servo system	16
1.7 Conclusions	17
 2 The locus of a perturbed relay system (LPRS) theory	 19
2.1 Introduction to the LPRS	19
2.2 Computing the LPRS for a non-integrating plant	21
2.2.1 Matrix state-space description approach	21
2.2.2 Partial fraction expansion technique	23
2.2.3 Transfer function description approach	24
2.2.4 Orbital stability of relay systems	26
2.3 Computing the LPRS for an integrating plant	26
2.3.1 Matrix state-space description approach	26
2.3.2 Transfer function description approach	29
2.3.3 Orbital stability of relay systems	30
2.4 Computing the LPRS for a plant with a time delay	31
2.4.1 Matrix state-space description approach	31
2.4.2 Orbital asymptotic stability	32
2.5 LPRS of first-order dynamics	33
2.6 LPRS of second-order dynamics	35

2.7	LPRS of first-order plus dead-time dynamics	38
2.8	Some properties of the LPRS	41
2.9	LPRS of nonlinear plants	43
2.9.1	Additivity property	43
2.9.2	The LPRS extended definition and open-loop LPRS computing	46
2.10	Application of periodic signal mapping to computing the LPRS of some special nonlinear plants	48
2.11	Comparison of the LPRS with other methods of analysis of relay systems	52
2.12	An example of analysis of oscillations and transfer properties ..	53
2.13	Conclusions	54
3	Input-output analysis of relay servo systems	57
3.1	Slow and fast signal propagation through a relay servo system	57
3.2	Methodology of input-output analysis	63
3.3	Example of forced motions analysis with the use of the LPRS ..	63
3.4	Conclusions	65
4	Analysis of sliding modes in the frequency domain	67
4.1	Introduction to sliding mode control	67
4.2	Representation of a sliding mode system via the equivalent relay system	69
4.3	Analysis of motions in the equivalent relay system	73
4.4	The chattering phenomenon and its LPRS analysis	77
4.5	Reduced-order and non-reduced-order models of averaged motions in a sliding mode system and input-output analysis ..	85
4.6	On fractal dynamics in sliding-mode control	88
4.7	Examples of chattering and disturbance attenuation analysis ..	95
4.8	Conclusions	101
5	Performance analysis of second-order SM control algorithms	103
5.1	Introduction	103
5.2	Sub-optimal algorithm	104
5.3	Describing function analysis of chattering	105
5.4	Exact frequency-domain analysis of chattering	106
5.5	Describing function analysis of external signal propagation	108
5.6	Exact frequency-domain analysis of external signal propagation	112
5.7	Example of the analysis of sub-optimal algorithm performance	117
5.8	Conclusions	122

Part II Applications of the locus of a perturbed relay system

6	Relay pneumatic servomechanism design	125
6.1	Relay pneumatic servomechanism dynamics and characteristics	125
6.2	LPRS analysis of uncompensated relay electro-pneumatic servomechanism	127
6.3	Compensator design in the relay electro-pneumatic servomechanism	128
6.4	Examples of compensator design in the relay electro-pneumatic servomechanism	132
6.5	Compensator design in the relay electro-pneumatic servomechanism with the use of the LPRS of a nonlinear plant	135
6.6	Conclusions	138
7	Relay feedback test identification and autotuning	139
7.1	The relay feedback test	139
7.2	The LPRS and asymmetric relay feedback test	140
7.3	Methodology of identification of the first-order plus dead-time process	141
7.4	Analysis of potential sources of inaccuracy	143
7.5	Performance analysis of the identification algorithm	145
7.6	Tuning algorithm	147
7.7	Conclusions	151
8	Performance analysis of the sliding mode-based analog differentiator and dynamical compensator	153
8.1	Transfer function "inversion" via sliding mode	153
8.2	Analysis of SM differentiator dynamics	154
8.3	Temperature sensor dynamics compensation via SM application	157
8.4	Analysis of the sliding mode compensator	160
8.5	An example of compensator design	162
8.6	Conclusions	165
9	Analysis of sliding mode observers	167
9.1	The SM observer as a relay servo system	167
9.2	SM observer performance analysis and characteristics	170
9.3	Example of SM observer performance analysis	172
9.4	Conclusions	175

10	Appendix	177
10.1	The LPRS derivation for a non-integrating linear part	177
10.2	Orbital stability of a system with a non-integrating linear part	181
10.3	The LPRS derivation for an integrating linear part	183
10.4	Orbital stability of a system with an integrating linear part	191
10.5	The LPRS derivation for a linear part with time delay	194
10.6	MATLAB code for LPRS computing	198
	References	205
	Index	211