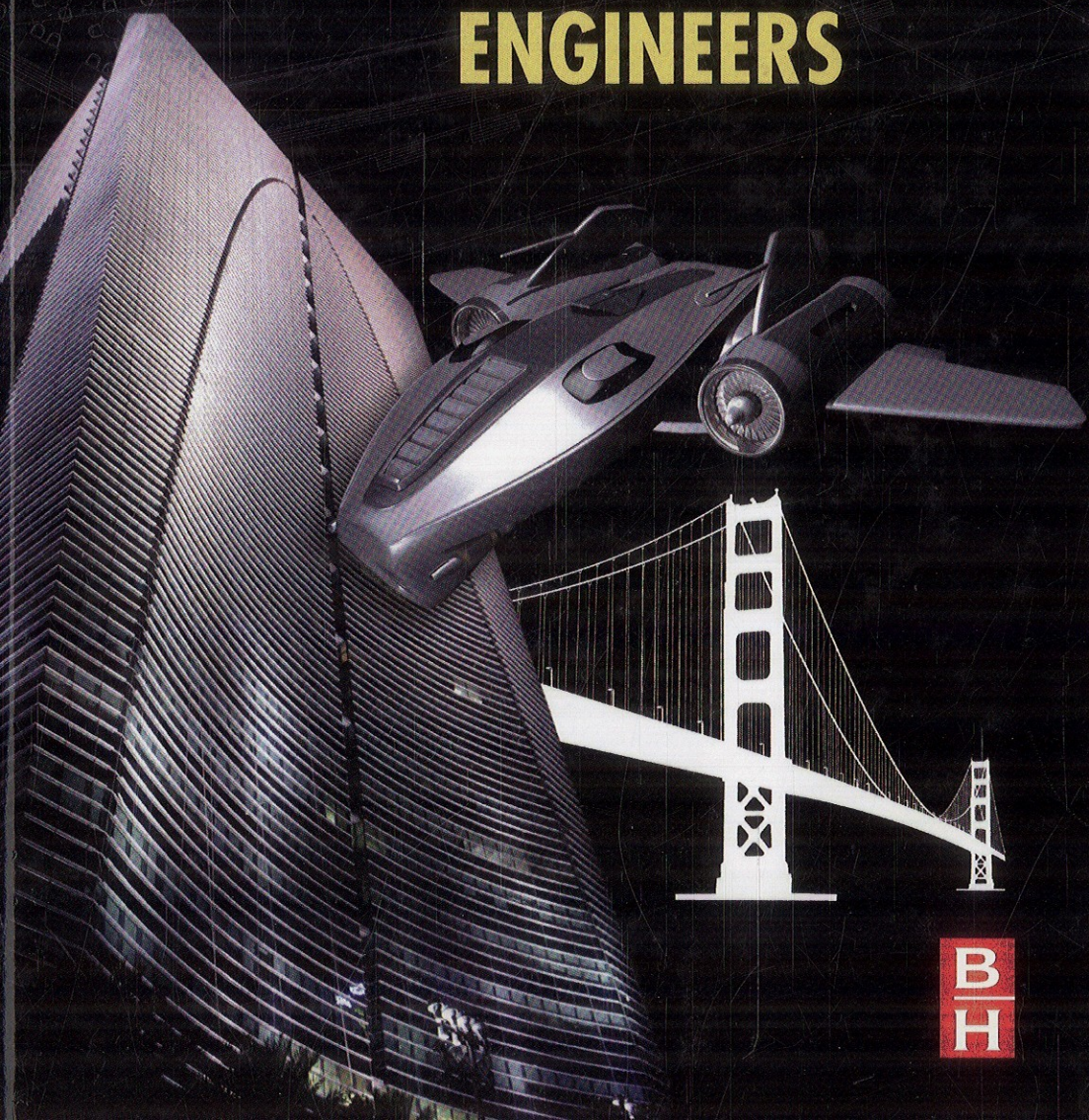


GIORA MAYMON

STRUCTURAL DYNAMICS AND PROBABILISTIC ANALYSES FOR ENGINEERS



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* A CD-ROM with all these files is attached to this publication.