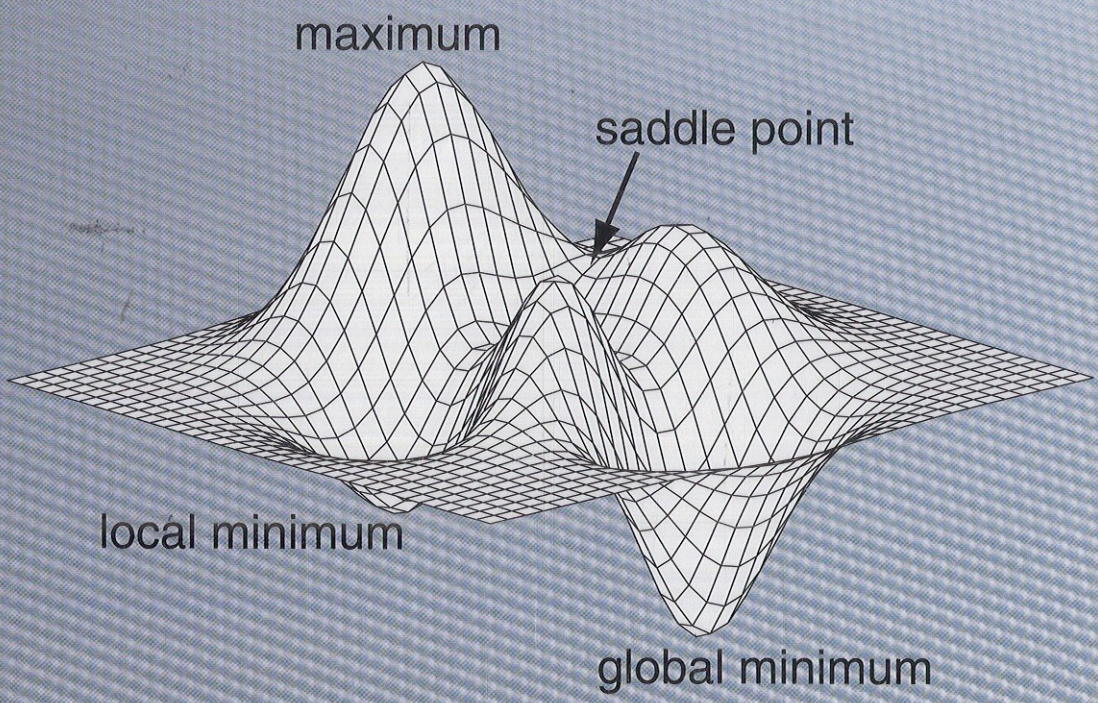
Wiley Series on Processing of Engineering Materials · Randall M. German, Series Editor

Materials Thermodynamics



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