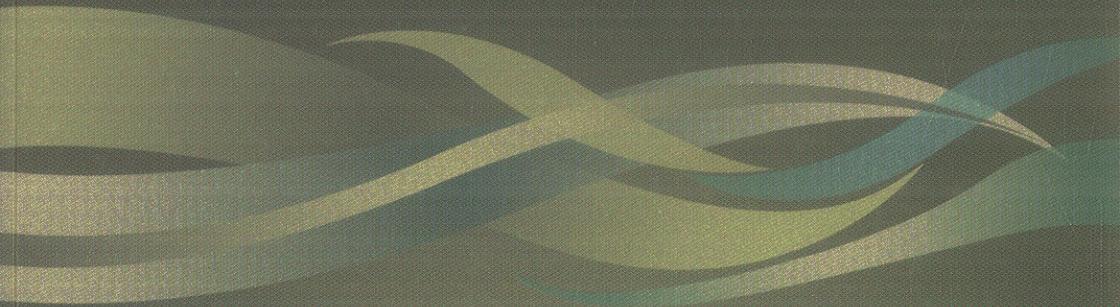


IISc Lecture Notes Series



Dilip P Patil
Uwe Storch

Introduction to Algebraic Geometry and Commutative Algebra



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