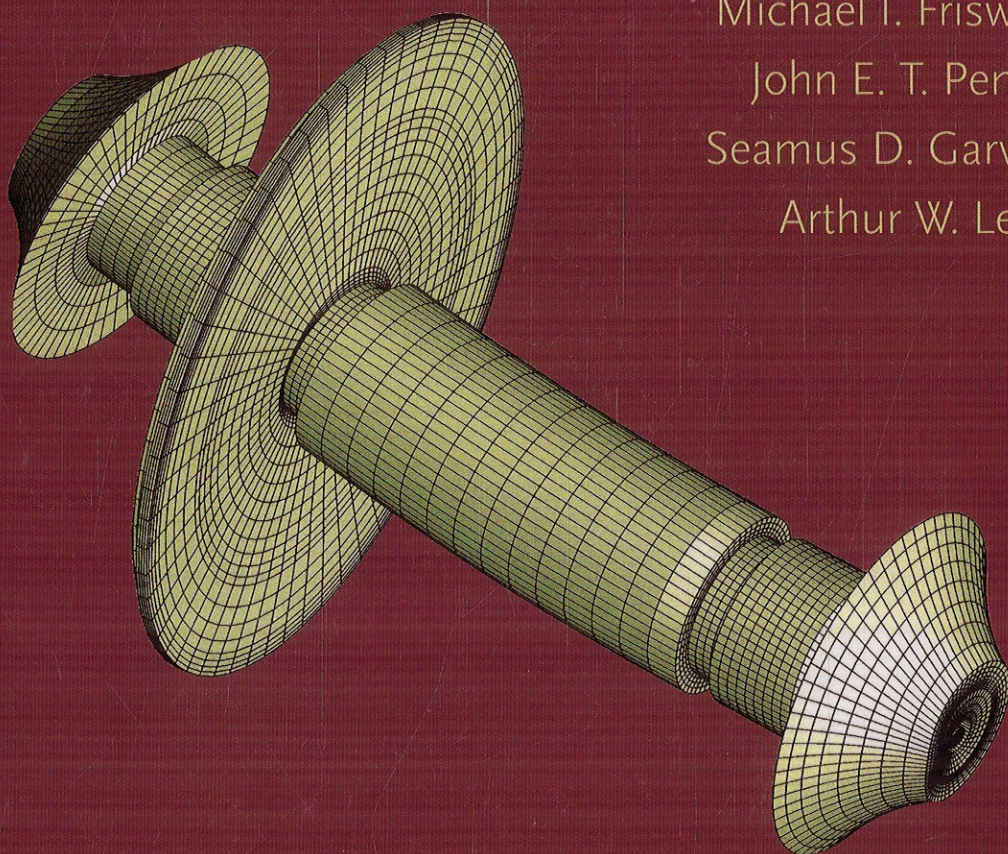


CAMBRIDGE
AEROSPACE
SERIES

DYNAMICS OF ROTATING MACHINES

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CAMBRIDGE

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