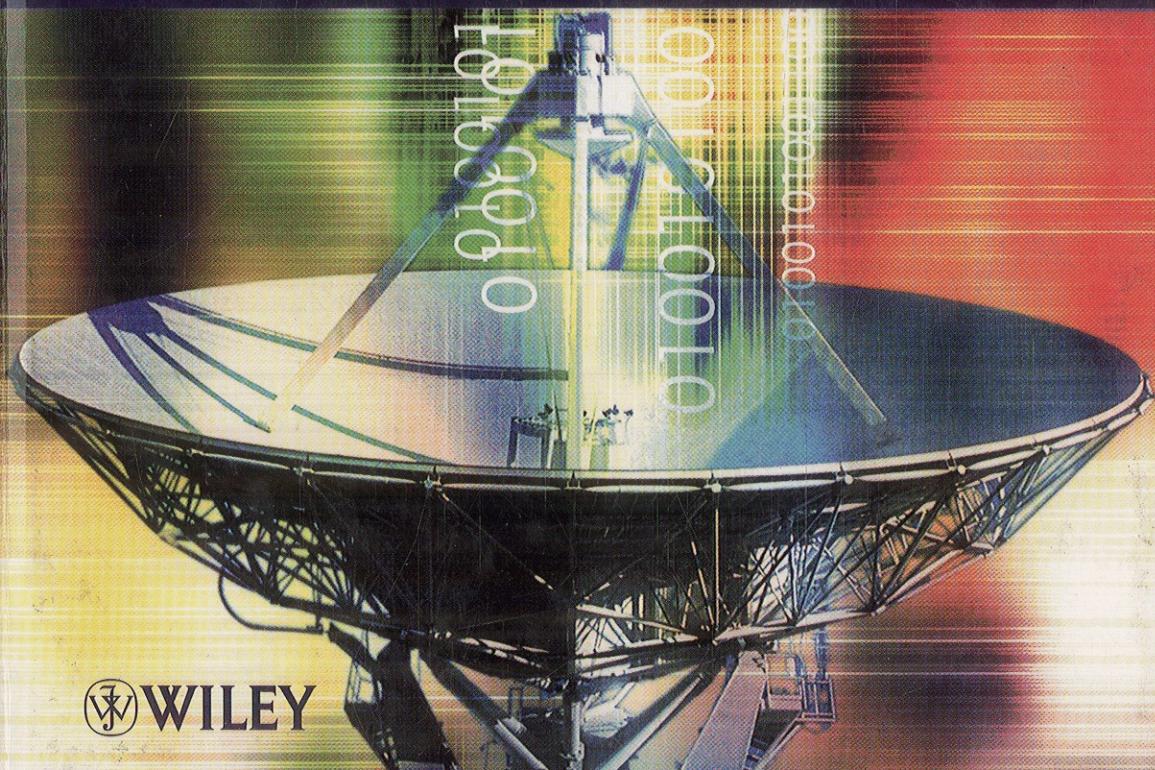


# MIMO RADAR SIGNAL PROCESSING

Edited by JIAN LI • PETRE STOICA



WILEY

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