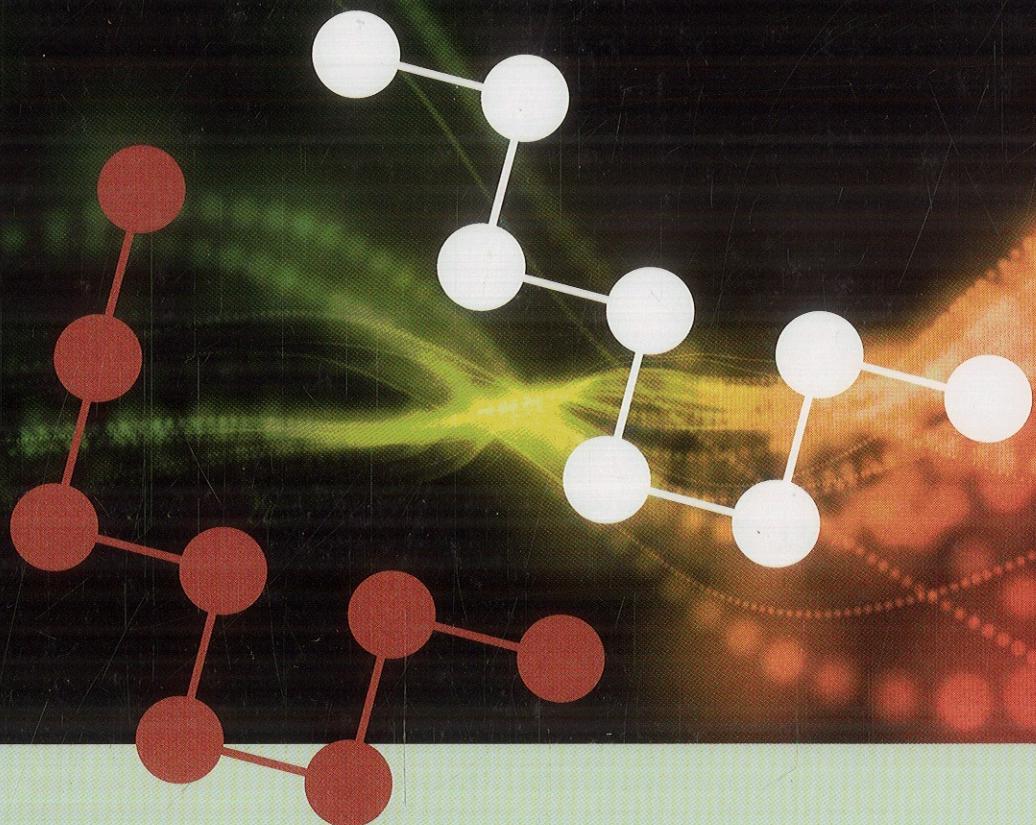


WILEY SERIES IN COMPUTATIONAL STATISTICS



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# ADVANCED MARKOV CHAIN MONTE CARLO METHODS

LEARNING FROM PAST SAMPLES

 WILEY

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