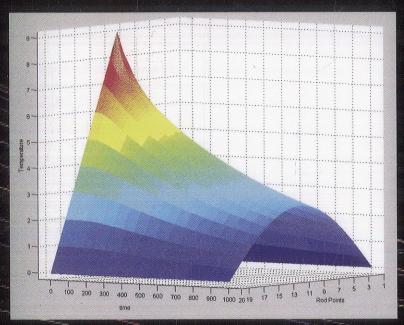
Chapman & Hall/CRC Computational Science Series

# the Simulation of Dynamics Using Simulink®



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A CHAPMAN & HALL BOOK

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