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 WILEY-VCH

Kinetic Processes

Crystal Growth, Diffusion, and Phase Transitions
in Materials

Second, Completely Revised and Enlarged Edition



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