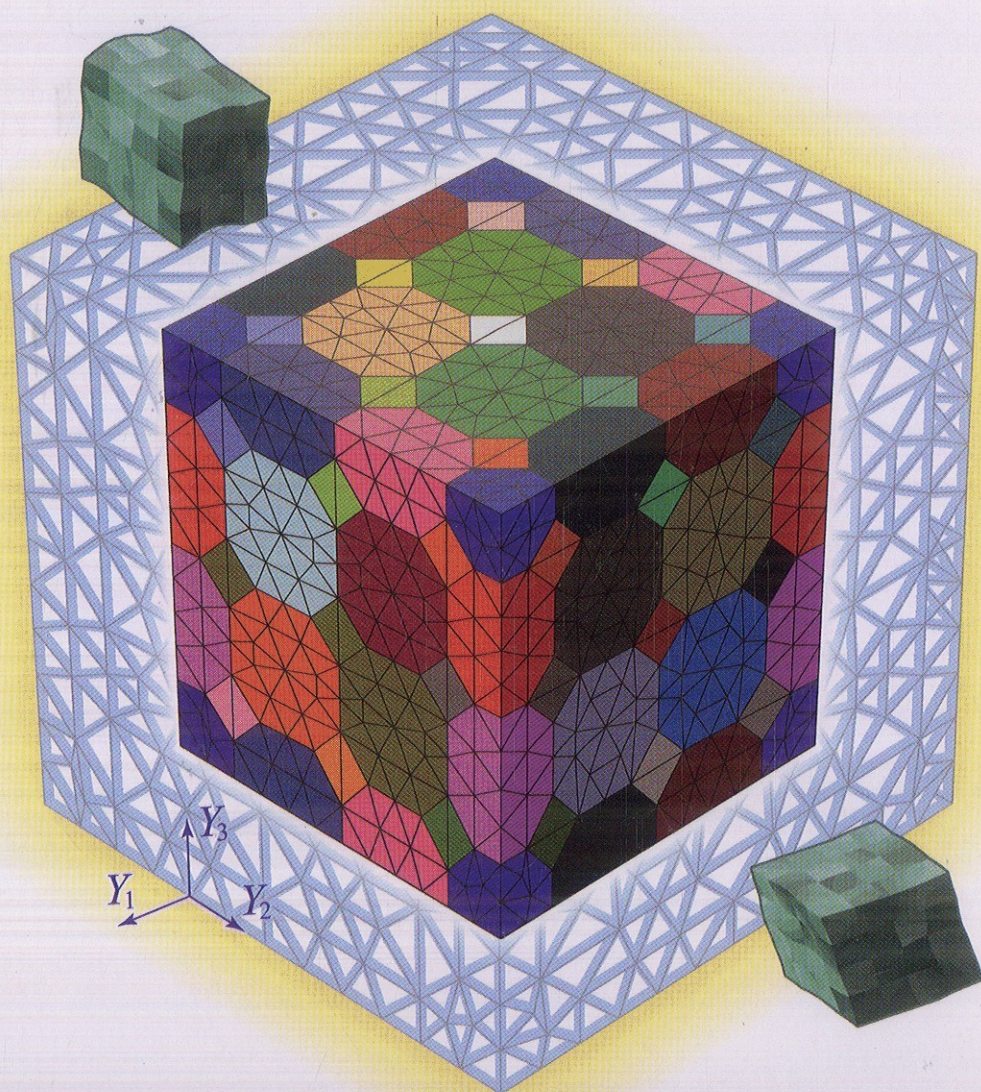


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Advanced Computational Materials Modeling

From Classical to Multi-Scale Techniques



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