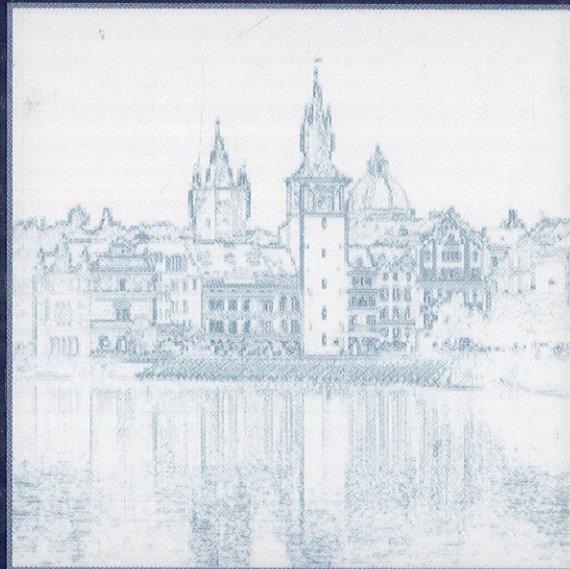
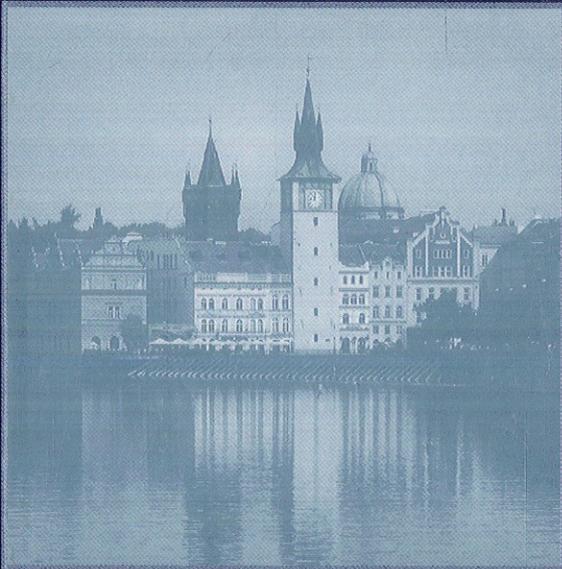


# WAVELET THEORY

*An Elementary Approach  
with Applications*

DAVID K. RUCH and PATRICK J. VAN FLEET



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