

K&E Series on Knots and Everything – Vol. 23

DIAMOND

A Paradox Logic

2nd Edition

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World Scientific

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