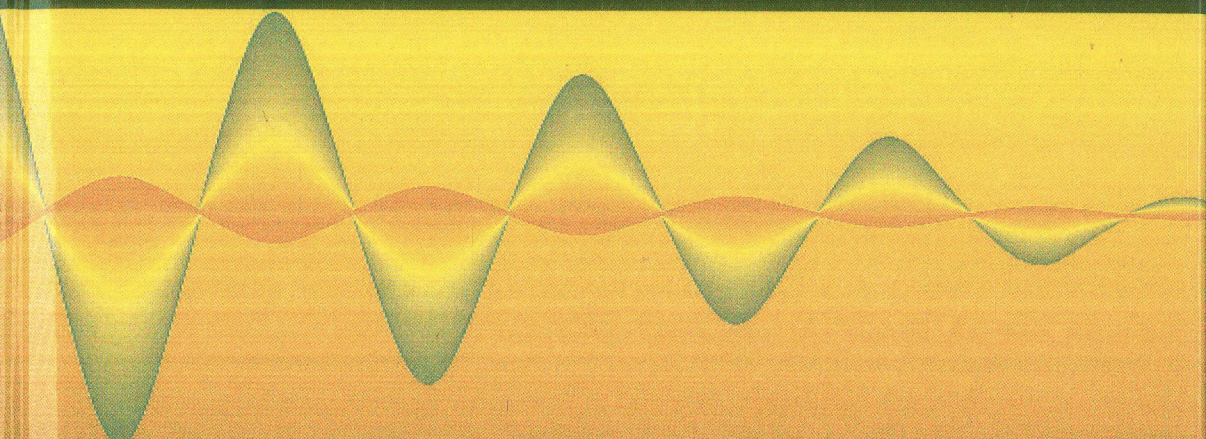


DSP

DIGITAL SIGNAL AND IMAGE PROCESSING SERIES



Discrete Stochastic Processes and Optimal Filtering

Second Edition

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ISTE

 **WILEY**

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