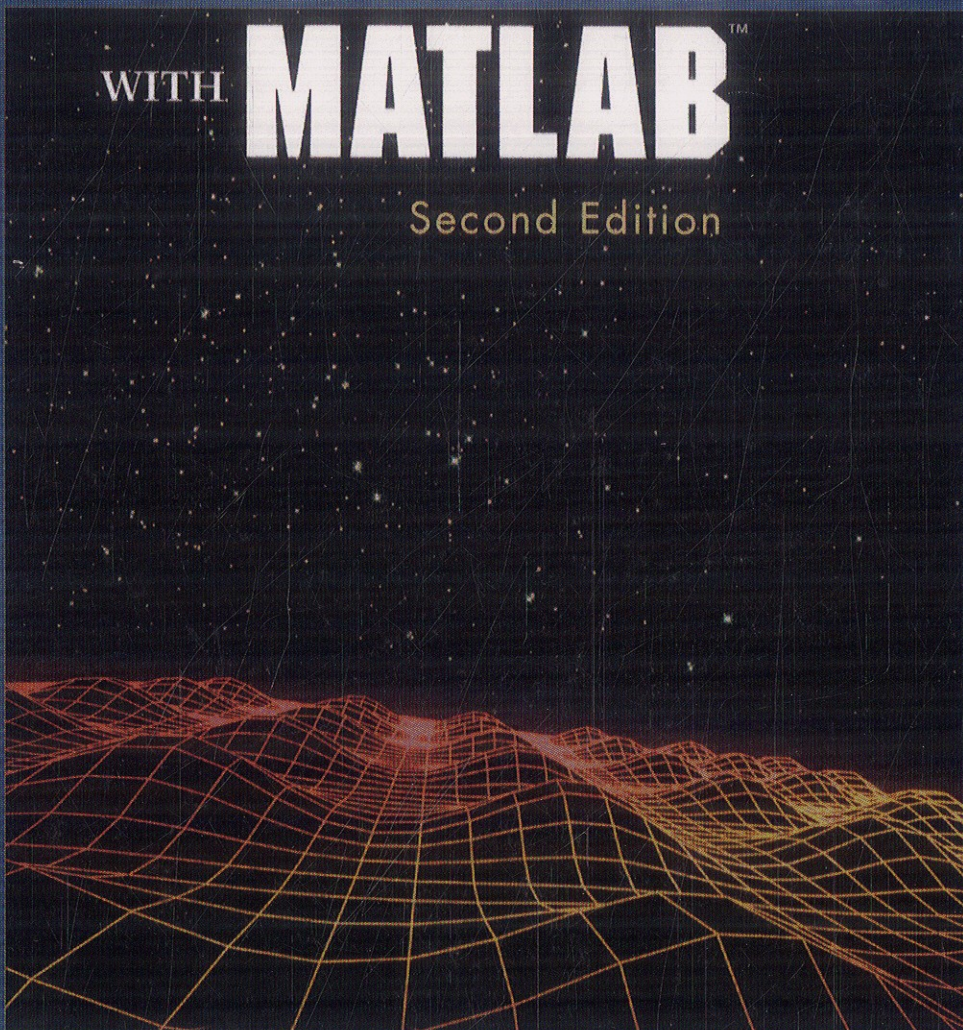


NUMERICAL ANALYSIS AND GRAPHIC VISUALIZATION

WITH **MATLAB**TM

Second Edition



SHOICHIRO NAKAMURA

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