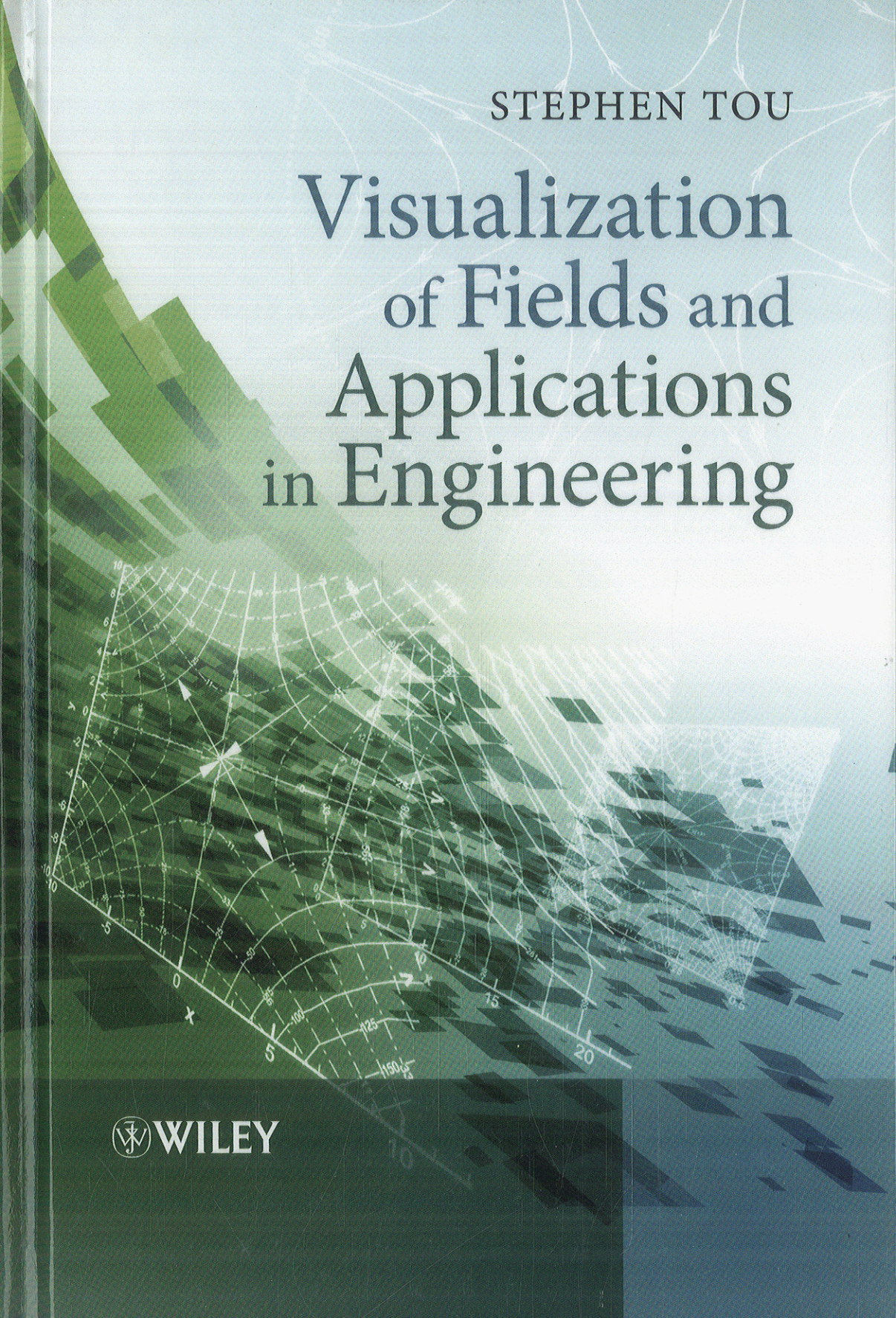


STEPHEN TOU

Visualization of Fields and Applications in Engineering



 WILEY

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