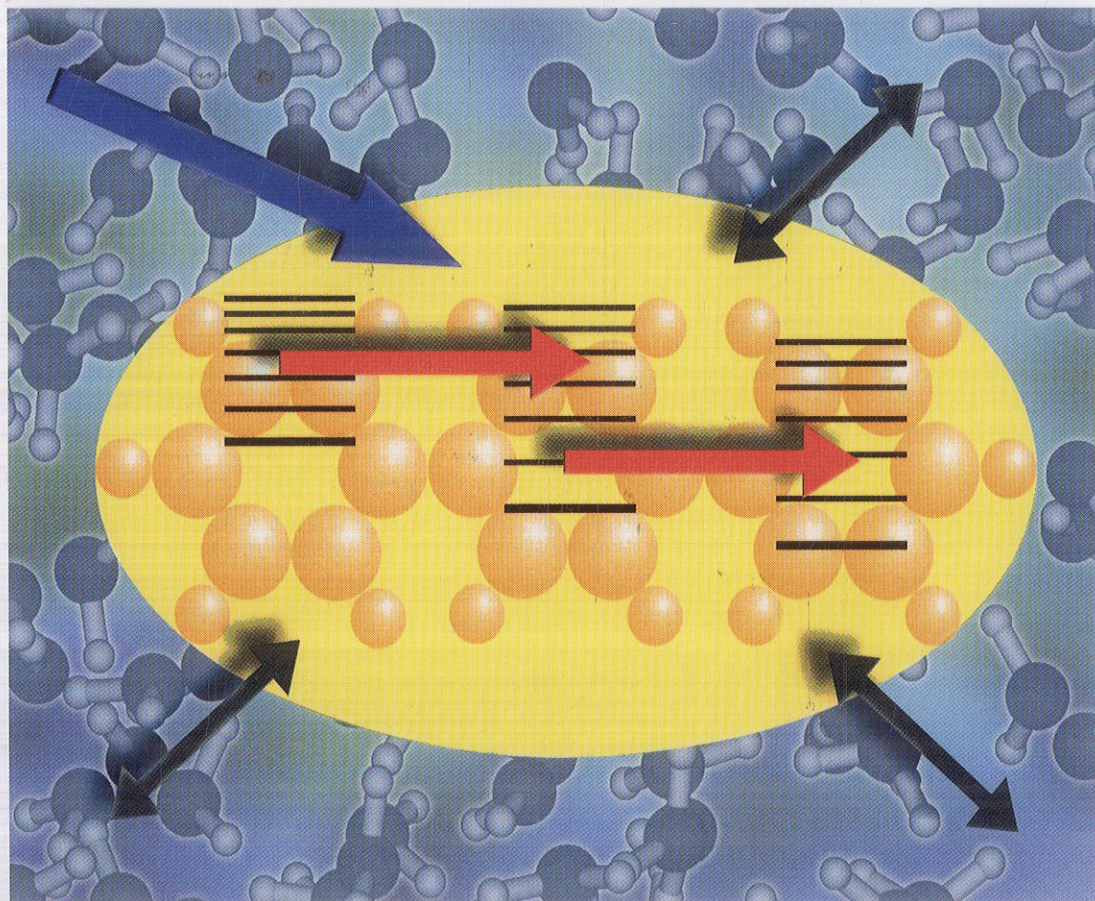


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# Charge and Energy Transfer Dynamics in Molecular Systems

Third, Revised and Enlarged Edition



# Contents

**Preface to the Third Edition** XIII

**Preface to the Second Edition** XV

**Preface to the First Edition** XVII

<b>1</b>	<b>Introduction</b>	<b>1</b>
<b>2</b>	<b>Electronic and Vibrational Molecular States</b>	<b>9</b>
2.1	Introduction	9
2.2	Molecular Schrödinger Equation	11
2.3	Born–Oppenheimer Separation	13
2.3.1	Born–Oppenheimer Approximation	15
2.3.2	Some Estimates	17
2.4	Electronic Structure Methods	18
2.4.1	The Hartree–Fock Equations	21
2.4.2	Density Functional Theory	23
2.5	Condensed Phase Approaches	24
2.5.1	Dielectric Continuum Model	25
2.5.2	Explicit Quantum-Classical Solvent Model	31
2.6	Potential Energy Surfaces	33
2.6.1	Harmonic Approximation and Normal Mode Analysis	35
2.6.2	Operator Representation of the Normal Mode Hamiltonian	39
2.6.3	Reaction Paths	44
2.7	Diabatic versus Adiabatic Representation of the Molecular Hamiltonian	50
2.8	Supplement	56
2.8.1	The Hartree–Fock Equations	56
2.8.2	Franck–Condon Factors	59
2.8.3	The Two-Level System	60
2.8.4	The Linear Molecular Chain and the Molecular Ring	64
	References	66
	Further Reading	66

<b>3</b>	<b>Dynamics of Isolated and Open Quantum Systems</b>	<b>67</b>
3.1	Introduction	67
3.2	Time-Dependent Schrödinger Equation	74
3.2.1	Wave Packets	74
3.2.2	The Interaction Representation	78
3.2.3	Multidimensional Wave Packet Dynamics	80
3.3	The Golden Rule of Quantum Mechanics	83
3.3.1	Transition from a Single State into a Continuum	84
3.3.2	Transition Rate for a Thermal Ensemble	87
3.3.3	Green's Function Approach	91
3.4	The Nonequilibrium Statistical Operator and the Density Matrix	94
3.4.1	The Density Operator	94
3.4.2	The Density Matrix	97
3.4.3	Equation of Motion for the Density Operator	99
3.4.4	Wigner Representation of the Density Operator	100
3.4.5	Dynamics of Coupled Multilevel Systems in a Heat Bath	103
3.5	The Reduced Density Operator and the Reduced Density Matrix	107
3.5.1	The Reduced Density Operator	107
3.5.2	Equation of Motion for the Reduced Density Operator	108
3.5.3	Mean-Field Approximation	109
3.5.4	The Interaction Representation of the Reduced Density Operator	111
3.5.5	The Projection Superoperator	112
3.5.6	Second-Order Equation of Motion for the Reduced Density Operator	115
3.6	The Reservoir Correlation Function	117
3.6.1	General Properties of $C_{uv}(t)$	117
3.6.2	Harmonic Oscillator Reservoir	120
3.6.3	The Spectral Density	122
3.6.4	Linear Response Theory for the Reservoir	125
3.6.5	Classical description of $C_{uv}(t)$	127
3.7	Quantum Master Equation	128
3.7.1	Markov Approximation	130
3.8	Reduced Density Matrix in Energy Representation	134
3.8.1	The Quantum Master Equation in Energy Representation	134
3.8.2	Multilevel Redfield Equations	136
3.8.3	The Secular Approximation	141
3.8.4	State Expansion of the System-Reservoir Coupling	142
3.8.5	From Coherent to Dissipative Dynamics: A Simple Example	144
3.8.6	Coordinate and Wigner Representation of the Reduced Density Matrix	150
3.9	Generalized Rate Equations: The Liouville Space Approach	153
3.9.1	Projection Operator Technique	154
3.9.2	Generalized Rate Equations	155
3.9.3	Rate Equations	157
3.9.4	The Memory Kernels	158
3.9.5	Second-Order Rate Expressions	160

3.9.6	Fourth-Order Rate Expressions	162
3.10	The Path Integral Representation of the Density Matrix	168
3.11	Quantum-Classical Hybrid Methods	174
3.11.1	The Mean-Field Approach	174
3.11.2	The Surface Hopping Method	176
3.11.3	Partial Wigner Representation as a Quantum-Classical Hybrid Method	179
3.12	Supplement	183
3.12.1	Different Equations of Motion for the Reduced Density Operator	183
3.12.2	Limit of Ultrashort Reservoir Correlation Time	187
3.12.3	Markov Approximation and the Factorized Part of the Reservoir Correlation Function	188
	References	189
	Further Reading	189
<b>4</b>	<b>Interaction of Molecular Systems with Radiation Fields</b>	<b>191</b>
4.1	Introduction	191
4.2	Absorption and Emission of Light	196
4.2.1	Linear Absorption Coefficient	196
4.2.2	Dipole-Dipole Correlation Function	197
4.2.3	Field Quantization and Spontaneous Emission of Light	199
4.3	Nonlinear Optical Response	202
4.3.1	Nonlinear Response Functions	205
4.4	Laser Control of Molecular Dynamics	206
4.4.1	Introduction	206
4.4.2	Optimal Control Theory	212
	References	219
	Further Reading	220
<b>5</b>	<b>Vibrational Dynamics: Energy Redistribution, Relaxation, and Dephasing</b>	<b>221</b>
5.1	Introduction	221
5.2	Intramolecular Vibrational Energy Redistribution	225
5.2.1	Zeroth-Order Basis	225
5.2.2	Golden Rule and Beyond	228
5.3	Intermolecular Vibrational Energy Relaxation	232
5.3.1	Diatomic Molecule in Solid State Environment	233
5.3.2	Diatomic Molecules in Polyatomic Solution	238
5.4	Polyatomic Molecules in Solution	243
5.4.1	System-Bath Hamiltonian	243
5.4.2	Higher-Order Multiquantum Relaxation	245
5.5	Quantum-Classical Approaches to Relaxation and Dephasing	250
5.6	Supplement	253
5.6.1	Coherent Wave Packet Motion in a Harmonic Oscillator	253
	References	254
	Further Reading	254



<b>6</b>	<b>Intramolecular Electronic Transitions</b>	<b>255</b>
6.1	Introduction	255
6.1.1	Optical Transitions	256
6.1.2	Internal Conversion Processes	261
6.2	The Optical Absorption Coefficient	262
6.2.1	Golden Rule Formulation	262
6.2.2	The Density of States	265
6.2.3	Absorption Coefficient for Harmonic Potential Energy Surfaces	268
6.2.4	Absorption Lineshape and Spectral Density	271
6.3	Absorption Coefficient and Dipole–Dipole Correlation Function	276
6.3.1	Absorption Coefficient and Wave Packet Propagation	276
6.3.2	Cumulant Expansion of the Absorption Coefficient	281
6.3.3	Absorption Coefficient and Reduced Density Operator Propagation	282
6.3.4	Mixed Quantum-Classical Computation of the Absorption Coefficient	285
6.4	The Emission Spectrum	287
6.5	Optical Preparation of an Excited Electronic State	288
6.5.1	Wave Function Formulation	289
6.5.2	Density Matrix Formulation	293
6.6	Pump–Probe Spectroscopy	294
6.7	Internal Conversion Dynamics	298
6.7.1	The Internal Conversion Rate	298
6.7.2	Ultrafast Internal Conversion	300
6.8	Supplement	302
6.8.1	Absorption Coefficient for Displaced Harmonic Oscillators	302
6.8.2	Cumulant Expansion for Harmonic Potential Energy Surfaces	305
	References	307
	Further Reading	307
<b>7</b>	<b>Electron Transfer</b>	<b>309</b>
7.1	Classification of Electron Transfer Reactions	309
7.2	Theoretical Models for Electron Transfer Systems	321
7.2.1	The Electron Transfer Hamiltonian	322
7.2.2	The Electron–Vibrational Hamiltonian of a Donor–Acceptor Complex	327
7.2.3	Electron–Vibrational State Representation of the Hamiltonian	331
7.3	Regimes of Electron Transfer	332
7.3.1	Landau–Zener Theory of Electron Transfer	337
7.4	Nonadiabatic Electron Transfer in a Donor–Acceptor Complex	341
7.4.1	High-Temperature Case	342
7.4.2	High-Temperature Case: Two Independent Sets of Vibrational Coordinates	346
7.4.3	Low-Temperature Case: Nuclear Tunneling	349
7.4.4	The Mixed Quantum-Classical Case	352

7.4.5	Description of the Mixed Quantum-Classical Case by a Spectral Density	354
7.5	Nonadiabatic Electron Transfer in Polar Solvents	355
7.5.1	The Solvent Polarization Field and the Dielectric Function	357
7.5.2	The Free Energy of the Solvent	360
7.5.3	The Rate of Nonadiabatic Electron Transfer in Polar Solvents	363
7.6	Bridge-Mediated Electron Transfer	367
7.6.1	The Superexchange Mechanism	369
7.6.2	Electron Transfer through Arbitrary Long Bridges	371
7.7	Nonequilibrium Quantum Statistical Description of Electron Transfer	375
7.7.1	Unified Description of Electron Transfer in a Donor–Bridge–Acceptor System	376
7.7.2	Transition to the Adiabatic Electron Transfer	379
7.8	Heterogeneous Electron Transfer	380
7.8.1	Nonadiabatic Charge Injection into the Solid State Described in a Single-Electron Model	381
7.8.2	Nonadiabatic Electron Transfer from the Solid State to the Molecule	385
7.8.3	Ultrafast Photoinduced Heterogeneous Electron Transfer from a Molecule into a Semiconductor	388
7.9	Charge Transmission through Single Molecules	390
7.9.1	Inelastic Charge Transmission	393
7.9.2	Elastic Charge Transmission	396
7.10	Photoinduced Ultrafast Electron Transfer	402
7.10.1	Quantum Master Equation for Electron Transfer Reactions	408
7.10.2	Rate Expressions	412
7.11	Controlling Photoinduced Electron Transfer	414
7.12	Supplement	417
7.12.1	Landau–Zener Transition Amplitude	417
7.12.2	The Multimode Marcus Formula	419
7.12.3	The Free Energy Functional of the Solvent Polarization	420
7.12.4	Second-Order Electron Transfer Rate	423
7.12.5	Fourth-Order Donor–Acceptor Transition Rate	425
7.12.6	Rate of Elastic Charge Transmission through a Single Molecule	428
	References	431
	Further Reading	432
<b>8</b>	<b>Proton Transfer</b>	<b>435</b>
8.1	Introduction	435
8.2	Proton Transfer Hamiltonian	440
8.2.1	Hydrogen Bonds	440
8.2.2	Reaction Surface Hamiltonian for Intramolecular Proton Transfer	444
8.2.3	Tunneling Splittings	445
8.2.4	Proton Transfer Hamiltonian in the Condensed Phase	450

8.3	Adiabatic Proton Transfer	453
8.4	Nonadiabatic Proton Transfer	456
8.5	The Intermediate Regime: From Quantum to Quantum-Classical Hybrid Methods	458
8.5.1	Multidimensional Wave Packet Dynamics	458
8.5.2	Surface Hopping	461
8.6	Infrared Laser-Pulse Control of Proton Transfer	463
	References	466
	Further Reading	466
<b>9</b>	<b>Excitation Energy Transfer</b>	<b>467</b>
9.1	Introduction	467
9.2	The Aggregate Hamiltonian	474
9.2.1	The Intermolecular Coulomb Interaction	477
9.2.2	The Two-Level Model	481
9.2.3	Single and Double Excitations of the Aggregate	484
9.2.4	Introduction of Delocalized Exciton States	490
9.3	Exciton-Vibrational Interaction	494
9.3.1	Exclusive Coupling to Intramolecular Vibrations	495
9.3.2	Coupling to Aggregate Normal-Mode Vibrations	495
9.3.3	Coupling to Intramolecular Vibrations and Aggregate Normal-Mode Vibrations	497
9.3.4	Exciton-Vibrational Hamiltonian and Excitonic Potential Energy Surfaces	498
9.4	Regimes of Excitation Energy Transfer	500
9.4.1	Quantum Statistical Approaches to Excitation Energy Transfer	501
9.5	Transfer Dynamics in the Case of Weak Excitonic Coupling: Förster Theory	503
9.5.1	The Transfer Rate	503
9.5.2	The Förster Rate	505
9.5.3	Nonequilibrium Quantum Statistical Description of Förster Transfer	508
9.6	Transfer Dynamics in the Case of Strong Excitonic Coupling	514
9.6.1	Rate Equations for Exciton Dynamics	515
9.6.2	Density Matrix Equations for Exciton Dynamics	516
9.6.3	Site Representation	519
9.6.4	Excitation Energy Transfer among Different Aggregates	521
9.6.5	Exciton Transfer in the Case of Strong Exciton-Vibrational Coupling	522
9.7	The Aggregate Absorption Coefficient	526
9.7.1	Case of no Exciton-Vibrational Coupling	529
9.7.2	Inclusion of Exciton-Vibrational Coupling	532
9.8	Excitation Energy Transfer Including Charge Transfer States	536
9.9	Exciton-Exciton Annihilation	540
9.9.1	Three-Level Description of the Molecules in the Aggregate	542
9.9.2	The Rate of Exciton-Exciton Annihilation	543

9.10	Supplement	544
9.10.1	Photon-Mediated Long-Range Excitation Energy Transfer	544
9.10.2	Fourth-Order Rate of Two-Electron-Transfer-Assisted EET	553
	References	557
	Further Reading	558
	<b>Index</b>	<b>559</b>