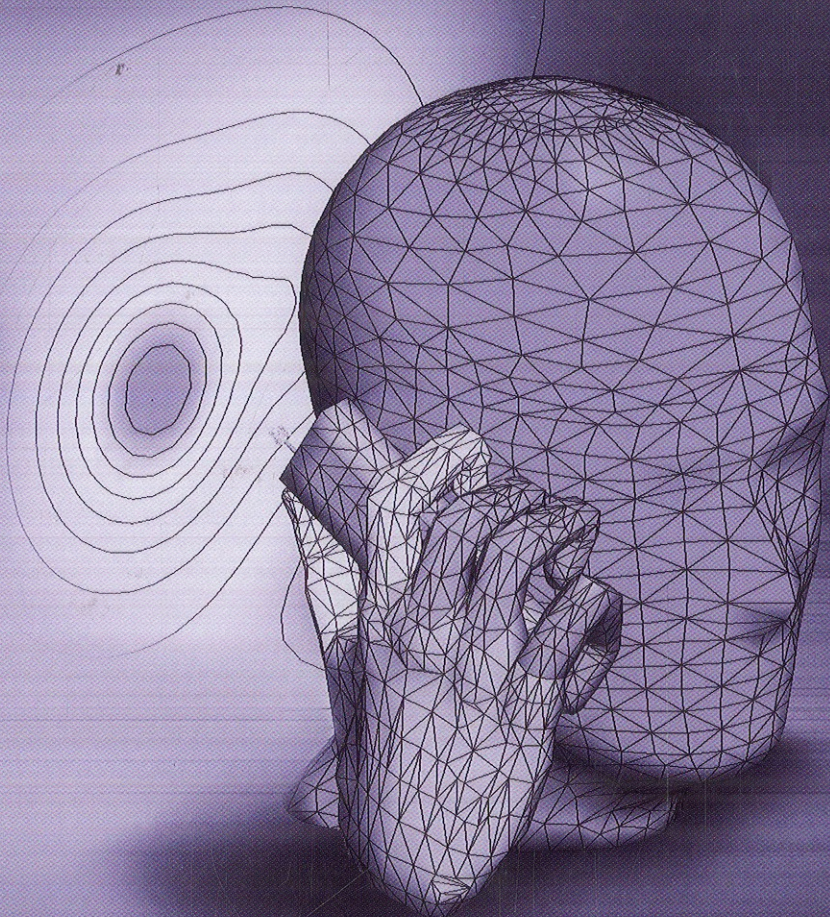


Computational Electromagnetics for RF and Microwave Engineering

Second Edition

David B. Davidson



CAMBRIDGE

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