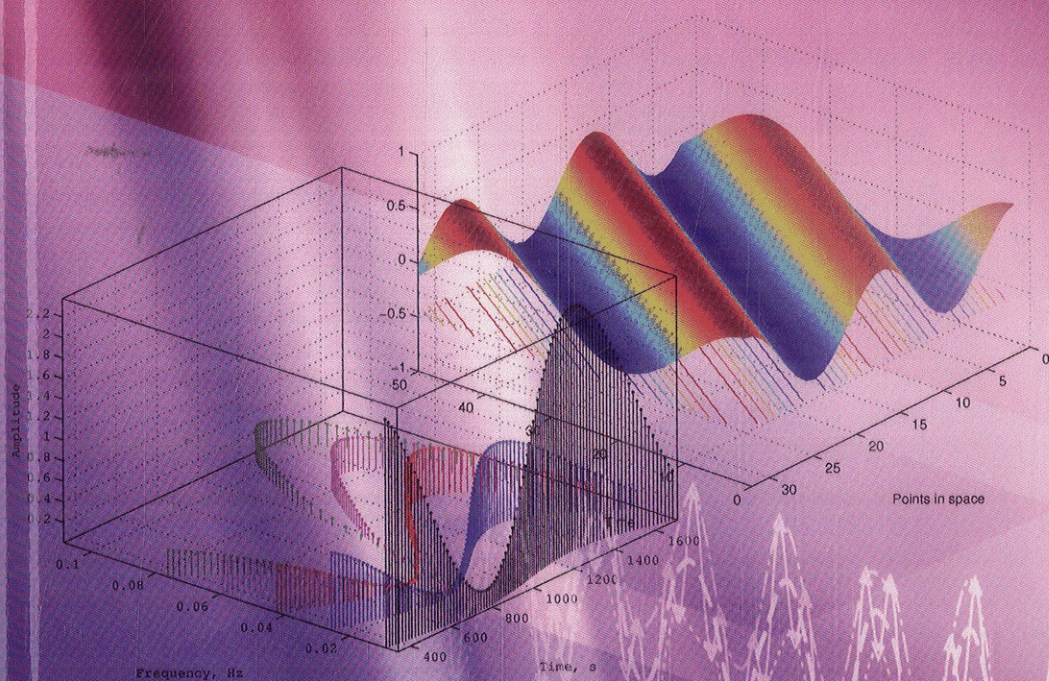


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HILBERT TRANSFORM APPLICATIONS IN MECHANICAL VIBRATION



 **WILEY**

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