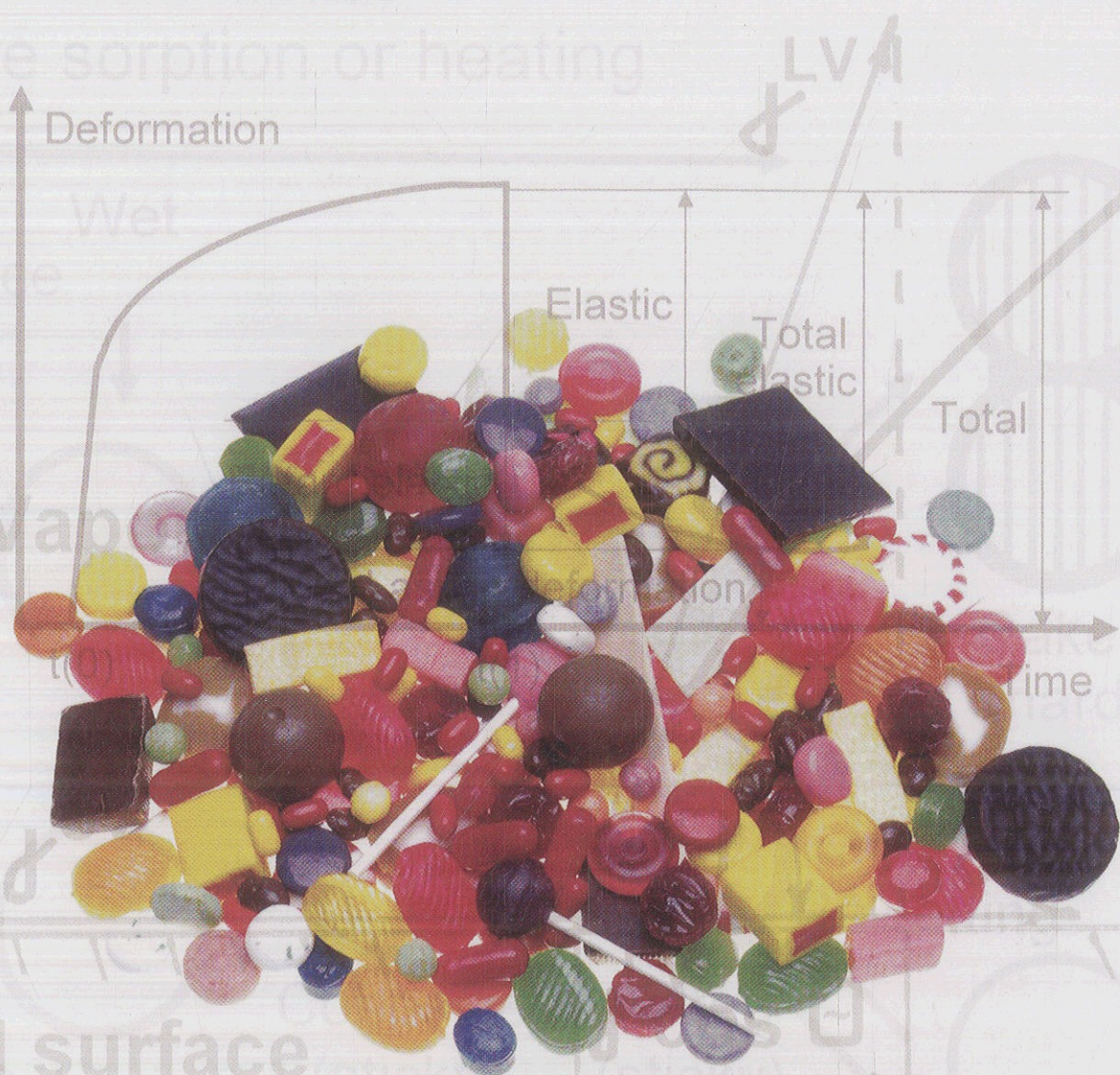


Confectionery and Chocolate Engineering

Principles and Applications

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Contents

<i>Preface</i>	<i>xviii</i>
<i>Acknowledgements</i>	<i>xxi</i>
Part I Theoretical introduction	1
Chapter 1 Principles of food engineering	3
1.1 Introduction	3
1.1.1 The peculiarities of food engineering	3
1.1.2 The hierarchical and semi-hierarchical structure of materials	5
1.1.3 Application of the Damköhler equations in food engineering	6
1.2 The Damköhler equations	6
1.3 Investigation of the Damköhler equations by means of similarity theory	8
1.3.1 Dimensionless numbers	8
1.3.2 Degrees of freedom of an operational unit	11
1.3.3 Polynomials as solutions of the Damköhler equations	12
1.4 Analogies	13
1.4.1 The Reynolds analogy	13
1.4.2 The Colburn analogy	15
1.4.3 Similarity and analogy	16
1.5 Dimensional analysis	16
1.6 The Buckingham Π theorem	17
Further reading	18
Chapter 2 Characterization of substances used in the confectionery industry	19
2.1 Qualitative characterization of substances	19
2.1.1 Principle of characterization	19
2.1.2 Structural formulae of confectionery products	20
2.1.3 Classification of confectionery products according to their characteristic phase conditions	27
2.1.4 Phase transitions – a bridge between sugar sweets and chocolate	28
2.2 Quantitative characterization of confectionery products	29
2.2.1 Composition of chocolates and compounds	29
2.2.2 Composition of sugar confectionery	35
2.2.3 Composition of biscuits, crackers and wafers	43
2.3 Preparation of recipes	45
2.3.1 Recipes and net/gross material consumption	45
2.3.2 Planning of material consumption	48

Chapter 3	Engineering properties of foods	52
3.1	Introduction	53
3.2	Density	53
3.2.1	Solids and powdered solids	54
3.2.2	Particle density	54
3.2.3	Bulk density and porosity	55
3.2.4	Loose bulk density	55
3.2.5	Dispersions of various kinds, and solutions	56
3.3	Fundamental functions of thermodynamics	56
3.3.1	Internal energy	56
3.3.2	Enthalpy	58
3.3.3	Specific heat capacity calculations	58
3.4	Latent heat and heat of reaction	62
3.4.1	Latent heat and free enthalpy	62
3.4.2	Phase transitions	63
3.5	Thermal conductivity	66
3.5.1	First Fourier equation	66
3.5.2	Heterogeneous materials	67
3.5.3	Liquid foods	67
3.5.4	Liquids containing suspended particles	68
3.5.5	Gases	68
3.6	Thermal diffusivity and Prandtl number	69
3.6.1	Second Fourier equation	69
3.6.2	Liquids and gases	69
3.6.3	Prandtl number	70
3.7	Mass diffusivity and Schmidt number	71
3.7.1	Law of mass diffusion (Fick's first law)	71
3.7.2	Mutual mass diffusion	72
3.7.3	Mass diffusion in liquids	72
3.7.4	Temperature dependence of diffusion	73
3.7.5	Mass diffusion in complex solid foodstuffs	74
3.7.6	Schmidt number	75
3.8	Dielectric properties	76
3.8.1	Radio frequency and microwave heating	76
3.8.2	Power absorption – the Lambert–Beer law	77
3.8.3	Microwave and radio frequency generators	78
3.8.4	Analytical applications	81
3.9	Electrical conductivity	81
3.9.1	Ohm's law	81
3.9.2	Electrical conductivity of metals and electrolytes; the Wiedemann–Franz law and Faraday's law	82
3.9.3	Electrical conductivity of materials used in confectionery	83
3.9.4	Ohmic heating technology	83
3.10	Infrared absorption properties	85
3.11	Physical characteristics of food powders	86
3.11.1	Classification of food powders	86
3.11.2	Surface activity	87
3.11.3	Effect of moisture content and anticaking agents	87

3.11.4	Mechanical strength, dust formation and explosibility index	88
3.11.5	Compressibility	89
3.11.6	Angle of repose	91
3.11.7	Flowability	91
3.11.8	Caking	92
3.11.9	Effect of anticaking agents	95
3.11.10	Segregation	95
	Further reading	96
Chapter 4	The rheology of foods and sweets	97
4.1	Rheology: its importance in the confectionery industry	98
4.2	Stress and strain	98
4.2.1	Stress tensor	98
4.2.2	Cauchy strain, Hencky strain and deformation tensor	100
4.2.3	Dilatational and deviatoric tensors; tensor invariants	103
4.2.4	Constitutive equations	104
4.3	Solid behaviour	105
4.3.1	Rigid body	105
4.3.2	Elastic body (or Hookean body/model)	105
4.3.3	Linear elastic and nonlinear elastic materials	107
4.3.4	Texture of chocolate	108
4.4	Fluid behaviour	109
4.4.1	Ideal fluids and Pascal bodies	109
4.4.2	Fluid behaviour in steady shear flow	109
4.4.3	Extensional flow	126
4.4.4	Viscoelastic functions	132
4.4.5	Oscillatory testing	141
4.4.6	Electrorheology	144
4.5	Viscosity of solutions	144
4.6	Viscosity of emulsions	146
4.6.1	Viscosity of dilute emulsions	146
4.6.2	Viscosity of concentrated emulsions	147
4.6.3	Rheological properties of flocculated emulsions	148
4.7	Viscosity of suspensions	149
4.8	Rheological properties of gels	151
4.8.1	Fractal structure of gels	151
4.8.2	Scaling behaviour of the elastic properties of colloidal gels	152
4.8.3	Classification of gels with respect to the nature of the structural elements	153
4.9	Rheological properties of sweets	156
4.9.1	Chocolate mass	156
4.9.2	Truffle mass	162
4.9.3	Praline mass	163
4.9.4	Fondant mass	163
4.9.5	Dessert masses	164
4.9.6	Nut brittle (croquante) masses	165
4.9.7	Whipped masses	166

4.10	Rheological properties of wheat flour doughs	166
4.10.1	Complex rheological models for describing food systems	166
4.10.2	Special testing methods for the rheological study of doughs	170
4.10.3	Studies of the consistency of dough	172
	Further reading	175
Chapter 5	Introduction to food colloids	176
5.1	The colloidal state	177
5.1.1	Colloids in the confectionery industry	177
5.1.2	The colloidal region	177
5.1.3	The various types of colloidal systems	179
5.2	Formation of colloids	179
5.2.1	Microphases	179
5.2.2	Macromolecules	180
5.2.3	Micelles	180
5.2.4	Disperse (or non-cohesive) and cohesive systems	180
5.2.5	Energy conditions for colloid formation	181
5.3	Properties of macromolecular colloids	182
5.3.1	Structural types	182
5.3.2	Interactions between dissolved macromolecules	184
5.3.3	Structural changes in solid polymers	184
5.4	Properties of colloids of association	188
5.4.1	Types of colloids of association	188
5.4.2	Parameters influencing the structure of micelles and the value of c_M	190
5.5	Properties of interfaces	190
5.5.1	Boundary layer and surface energy	190
5.5.2	Formation of boundary layer: adsorption	190
5.5.3	Dependence of interfacial energy on surface morphology	191
5.5.4	Phenomena when phases are in contact	193
5.5.5	Adsorption on the free surface of a liquid	196
5.6	Electrical properties of interfaces	198
5.6.1	The electric double layer and electrokinetic phenomena	198
5.6.2	Structure of the electric double layer	199
5.7	Theory of colloidal stability: the DLVO theory	200
5.8	Stability and changes of colloids and coarse dispersions	203
5.8.1	Stability of emulsions	203
5.8.2	Two-phase emulsions	205
5.8.3	Three-phase emulsions	205
5.8.4	Two liquid phases plus a solid phase	205
5.8.5	Emulsifying properties of food proteins	207
5.8.6	Emulsion droplet size data and the kinetics of emulsification	207
5.8.7	Bancroft's rule for the type of emulsion	209
5.8.8	HLB value and stabilization of emulsions	210
5.8.9	Emulsifiers used in the confectionery industry	211
5.9	Emulsion instability	212
5.9.1	Mechanisms of destabilization	212
5.9.2	Flocculation	213
5.9.3	Sedimentation (creaming)	215

5.9.4	Coalescence	219
5.9.5	Ostwald ripening in emulsions	220
5.10	Phase inversion	221
5.11	Foams	222
5.11.1	Transient and metastable (permanent) foams	222
5.11.2	Expansion ratio and dispersity	224
5.11.3	Disproportionation	225
5.11.4	Foam stability: coefficient of stability and lifetime histogram	229
5.11.5	Stability of polyhedral foams	230
5.11.6	Thinning of foam films and foam drainage	230
5.11.7	Methods of improving foam stability	231
	Further reading	233

Part II Physical operations 235

Chapter 6	Comminution	237
6.1	Changes during size reduction	238
6.1.1	Comminution of non-cellular and cellular substances	238
6.1.2	Grinding and crushing	238
6.1.3	Dry and wet grinding	239
6.2	Rittinger's 'surface' theory	239
6.3	Kick's 'volume' theory	240
6.4	The third, or Bond, theory	241
6.5	Energy requirement for comminution	241
6.5.1	Work index	241
6.5.2	Differential equation for the energy requirement for comminution	241
6.6	Particle size distribution of ground products	242
6.6.1	Particle size	242
6.6.2	Screening	243
6.6.3	Sedimentation analysis	245
6.6.4	Electrical-sensing-zone method of particle size distribution determination (Coulter method)	245
6.7	Particle size distributions	245
6.7.1	Rosin-Rammler (RR) distribution	245
6.7.2	Normal distribution (Gaussian distribution, N distribution)	246
6.7.3	Log-normal (LN) distribution (Kolmogorov distribution)	246
6.7.4	Gates-Gaudin-Schumann (GGS) distribution	247
6.8	Kinetics of grinding	247
6.9	Comminution by five-roll refiners	248
6.9.1	Effect of a five-roll refiner on particles	248
6.9.2	Volume and mass flow in a five-roll refiner	251
6.10	Grinding by a melangeur	253
6.11	Comminution by a stirred ball mill	256
6.11.1	Kinetics of comminution in a stirred ball mill	257
6.11.2	Power requirement of a stirred ball mill	257
6.11.3	Residence time distribution in a stirred ball mill	259
	Further reading	261

Chapter 7	Mixing/kneading	263
7.1	Technical solutions to the problem of mixing	263
7.2	Power characteristics of a stirrer	264
7.3	Mixing-time characteristics of a stirrer	266
7.4	Representative shear rate and viscosity for mixing	266
7.5	Calculation of the Reynolds number for mixing	266
7.6	Mixing of powders	267
7.6.1	Degree of heterogeneity of a mixture	267
7.6.2	Scaling up of agitated centrifugal mixers	271
7.6.3	Mixing time for powders	272
7.6.4	Power consumption	273
7.7	Mixing of fluids of high viscosity	274
7.8	Effect of impeller speed on heat and mass transfer	275
7.8.1	Heat transfer	275
7.8.2	Mass transfer	275
7.9	Mixing by blade mixers	276
7.10	Mixing rolls	277
7.11	Mixing of two liquids	277
	Further reading	278
Chapter 8	Solutions	279
8.1	Preparation of aqueous solutions of carbohydrates	279
8.1.1	Mass balance	279
8.1.2	Parameters characterizing carbohydrate solutions	280
8.2	Solubility of sucrose in water	282
8.2.1	Solubility number of sucrose	282
8.3	Aqueous solutions of sucrose and glucose syrup	283
8.3.1	Syrup ratio	283
8.4	Aqueous sucrose solutions containing invert sugar	285
8.5	Solubility of sucrose in the presence of starch syrup and invert sugar	285
8.6	Rate of dissolution	286
	Further reading	288
Chapter 9	Evaporation	289
9.1	Theoretical background – Raoult's law	289
9.2	Boiling point of sucrose/water solutions at atmospheric pressure	291
9.3	Application of a modification of Raoult's law to calculate the boiling point of carbohydrate/water solutions at decreased pressure	291
9.3.1	Sucrose/water solutions	291
9.3.2	Dextrose/water solutions	292
9.3.3	Starch syrup/water solutions	292
9.3.4	Invert sugar solutions	292
9.3.5	Approximate formulae for the elevation of the boiling point of aqueous sugar solutions	292
9.4	Vapour pressure formulae for carbohydrate/water solutions	295
9.4.1	Vapour pressure formulae	295
9.4.2	Antoine's rule	297
9.4.3	Trouton's rule	299

9.4.4	Ramsay–Young rule	301
9.4.5	Dühring's rule	302
9.5	Practical tests for controlling the boiling points of sucrose solutions	303
9.6	Modelling of an industrial cooking process for chewy candy	304
9.6.1	Modelling of evaporation stage	305
9.6.2	Modelling of drying stage	307
	Further reading	307

Chapter 10 Crystallization 309

10.1	Introduction	310
10.2	Crystallization from solution	310
10.2.1	Nucleation	310
10.2.2	Supersaturation	311
10.2.3	Thermodynamic driving force for crystallization	312
10.2.4	Metastable state of a supersaturated solution	313
10.2.5	Nucleation kinetics	315
10.2.6	Thermal history of the solution	317
10.2.7	Secondary nucleation	318
10.2.8	Crystal growth	319
10.2.9	Theories of crystal growth	322
10.2.10	Effect of temperature on growth rate	323
10.2.11	Dependence of growth rate on the hydrodynamic conditions	324
10.2.12	Modelling of fondant manufacture based on the diffusion theory	326
10.3	Crystallization from melts	329
10.3.1	Polymer crystallization	329
10.3.2	Spherulite nucleation, spherulite growth and crystal thickening	330
10.3.3	Melting of polymers	333
10.3.4	Isothermal crystallization	334
10.3.5	Non-isothermal crystallization	345
10.3.6	Secondary crystallization	346
10.4	Crystal size distributions	346
10.4.1	Normal distribution	346
10.4.2	Log-normal distribution	346
10.4.3	Gamma distribution	347
10.4.4	Histograms and population balance	347
10.5	Batch crystallization	349
10.6	Isothermal and non-isothermal recrystallization	350
10.6.1	Ostwald ripening	350
10.6.2	Recrystallization under the effect of temperature or concentration fluctuations	351
10.6.3	Ageing	351
10.7	Methods for studying the supermolecular structure of fat melts	351
10.7.1	Cooling/solidification curve	351
10.7.2	Solid fat content	352
10.7.3	Dilatation: Solid fat index	353
10.7.4	Differential scanning calorimetry, differential thermal analysis and low-resolution NMR methods	354

10.8	Crystallization of glycerol esters: Polymorphism	355
10.9	Crystallization of cocoa butter	359
10.9.1	Polymorphism of cocoa butter	359
10.9.2	Tempering of cocoa butter and chocolate mass	360
10.9.3	Shaping (moulding) and cooling of cocoa butter and chocolate	365
10.9.4	Sugar blooming and dew point temperature	367
10.9.5	Crystallization during storage of chocolate products	368
10.9.6	Bloom inhibition	370
10.9.7	Tempering of cocoa powder	371
10.10	Crystallization of fat masses	371
10.10.1	Fat masses and their applications	371
10.10.2	Cocoa butter equivalents and improvers	372
10.10.3	Fats for compounds and coatings	374
10.10.4	Cocoa butter replacers	376
10.10.5	Cocoa butter substitutes	378
10.10.6	Filling fats	379
10.10.7	Fats for ice cream coatings and ice dippings/toppings	381
10.11	Crystallization of confectionery fats with a high trans-fat portion	382
10.11.1	Coating fats and coatings	383
10.11.2	Filling fats and fillings	383
10.11.3	Future trends in the manufacture of trans-free special confectionery fats	384
10.12	Modelling of chocolate cooling processes and tempering	385
10.12.1	Franke model for the cooling of chocolate coatings	385
10.12.2	Modelling the temperature distribution in cooling chocolate moulds	386
10.12.3	Modelling of chocolate tempering process	390
	Further reading	392
Chapter 11	Gelling, emulsifying, stabilizing and foam formation	394
11.1	Hydrocolloids used in confectionery	395
11.2	Agar	395
11.2.1	Isolation of agar	395
11.2.2	Types of agar	396
11.2.3	Solution properties	396
11.2.4	Gel properties	397
11.2.5	Setting point of sol and melting point of gel	398
11.2.6	Syneresis of an agar gel	398
11.2.7	Technology of manufacturing agar gels	399
11.3	Alginates	400
11.3.1	Isolation and structure of alginates	400
11.3.2	Mechanism of gelation	401
11.3.3	Preparation of a gel	401
11.3.4	Fields of application	402
11.4	Carrageenans	402
11.4.1	Isolation and structure of carrageenans	402
11.4.2	Solution properties	403

11.4.3	Depolymerization of carrageenan	404
11.4.4	Gel formation and hysteresis	405
11.4.5	Setting temperature and syneresis	405
11.4.6	Specific interactions	405
11.4.7	Utilization	406
11.5	Furcellaran	407
11.6	Gum arabic	407
11.7	Gum tragacanth	408
11.8	Guaran gum	408
11.9	Locust bean gum	409
11.10	Pectin	409
11.10.1	Isolation and composition of pectin	409
11.10.2	High-methoxyl (HM) pectins	410
11.10.3	Low-methoxyl (LM) pectins	411
11.10.4	Low-methoxyl (LM) amidated pectins	411
11.10.5	Gelling mechanisms	411
11.10.6	Technology of manufacturing pectin jellies	412
11.11	Starch	413
11.11.1	Occurrence and composition of starch	413
11.11.2	Modified starches	414
11.11.3	Utilization in the confectionery industry	414
11.12	Xanthan gum	416
11.13	Gelatin	416
11.13.1	Occurrence and composition of gelatin	416
11.13.2	Solubility	417
11.13.3	Gel formation	417
11.13.4	Viscosity	418
11.13.5	Amphoteric properties	418
11.13.6	Surface-active/protective-colloid properties and utilization	419
11.13.7	Methods of dissolution	420
11.13.8	Stability of gelatin solutions	421
11.13.9	Confectionery applications	421
11.14	Egg proteins	422
11.14.1	Fields of application	422
11.14.2	Structure	422
11.14.3	Egg-white gels	423
11.14.4	Egg-white foams	424
11.14.5	Egg-yolk gels	424
11.14.6	Whole-egg gels	425
11.15	Foam formation	425
11.15.1	Fields of application	425
11.15.2	Velocity of bubble rise	426
11.15.3	Whipping	429
11.15.4	Continuous industrial aeration	430
11.15.5	Industrial foaming methods	432
11.15.6	<i>In situ</i> generation of foam	432
	Further reading	433

Chapter 12	Transport	434
12.1	Types of transport	434
12.2	Calculation of flow rate of non-Newtonian fluids	434
12.3	Transporting dessert masses in long pipes	436
12.4	Changes in pipe direction	437
12.5	Laminar unsteady flow	438
12.6	Transport of flour and sugar by air flow	438
12.6.1	Physical parameters of air	438
12.6.2	Air flow in a tube	438
12.6.3	Flow properties of transported powders	439
12.6.4	Power requirement of air flow	441
12.6.5	Measurement of a pneumatic system	442
	Further reading	444
Chapter 13	Pressing	445
13.1	Applications of pressing in the confectionery industry	445
13.2	Theory of pressing	445
13.3	Cocoa liquor pressing	448
	Further reading	449
Chapter 14	Extrusion	451
14.1	Flow through a converging die	451
14.1.1	Theoretical principles of the dimensioning of extruders	451
14.1.2	Pressure loss in the shaping of pastes	455
14.1.3	Design of converging die	456
14.2	Feeders used for shaping confectionery pastes	459
14.2.1	Screw feeders	459
14.2.2	Cog-wheel feeders	460
14.2.3	Screw mixers and extruders	461
14.3	Extrusion cooking	464
14.4	Roller extrusion	465
14.4.1	Roller extrusion of biscuit doughs	465
14.4.2	Feeding by roller extrusion	467
	Further reading	467
Chapter 15	Particle agglomeration: Instantization and tableting	469
15.1	Theoretical background	469
15.1.1	Processes resulting from particle agglomeration	469
15.1.2	Solidity of a granule	472
15.1.3	Capillary attractive forces in the case of liquid bridges	472
15.1.4	Capillary attractive forces in the case of no liquid bridges	473
15.1.5	Solidity of a granule in the case of dry granulation	474
15.1.6	Water sorption properties of particles	475
15.1.7	Effect of electrostatic forces on the solidity of a granule	477
15.1.8	Effect of crystal bridges on the solidity of a granule	478
15.1.9	Comparison of the various attractive forces affecting granulation	479
15.1.10	Effect of surface roughness on the attractive forces	479

15.2	Processes of agglomeration	481
15.2.1	Agglomeration in the confectionery industry	481
15.2.2	Agglomeration from liquid phase	481
15.2.3	Agglomeration of powders: Tableting or dry granulation	482
15.3	Granulation by fluidization	482
15.3.1	Instantization by granulation: Wetting of particles	482
15.3.2	Processes of fluidization	483
15.4	Tabletting	484
15.4.1	Tablets as sweets	484
15.4.2	Types of tabletting	485
15.4.3	Compression, consolidation and compaction	486
15.4.4	Characteristics of the compaction process	488
15.4.5	Quality properties of tablets	492
	Further reading	492

Part III Chemical and complex operations: Stability of sweets 493

Chapter 16 Chemical operations (inversion and caramelization), ripening and complex operations 495

16.1	Inversion	495
16.1.1	Hydrolysis of sucrose by the effect of acids	495
16.1.2	A specific type of acidic inversion: Inversion by cream of tartar	498
16.1.3	Enzymatic inversion	499
16.2	Caramelization	502
16.2.1	Maillard reaction	502
16.2.2	Sugar melting	504
16.3	Alkalization of cocoa material	505
16.3.1	Purposes and methods of alkalization	505
16.3.2	German process	506
16.4	Ripening	507
16.4.1	Ripening processes of diffusion	507
16.4.2	Chemical and enzymatic reactions during ripening	509
16.5	Complex operations	510
16.5.1	Complexity of the operations used in the confectionery industry	510
16.5.2	Conching	510
16.5.3	New trends in the manufacture of chocolate	521
16.5.4	Modelling the structure of dough	522
	Further reading	523

Chapter 17 Water activity, shelf life and storage 525

17.1	Water activity	525
17.1.1	Definition of water activity	525
17.1.2	Adsorption/desorption of water	527
17.1.3	Measurement of water activity	527
17.1.4	Factors lowering water activity	533
17.1.5	Sorption isotherms	534

17.1.6	Hygroscopicity of confectionery products	535
17.1.7	Calculation of equilibrium relative humidity of confectionery products	538
17.2	Shelf life and storage	541
17.2.1	Definition of shelf life	541
17.2.2	Role of light and atmospheric oxygen	541
17.2.3	Role of temperature	541
17.2.4	Role of water activity	541
17.2.5	Role of enzymatic activity	542
17.2.6	Concept of mould-free shelf life	542
17.3	Storage scheduling	547
	Further reading	548
Chapter 18 Stability of food systems		550
18.1	Common use of the concept of food stability	550
18.2	Stability theories: types of stability	550
18.2.1	Orbital stability and Lyapunov stability	550
18.2.2	Asymptotic and marginal (or Lyapunov) stability	551
18.2.3	Local and global stability	552
18.3	Shelf life as a case of marginal stability	552
18.4	Stability matrix of a food system	553
18.4.1	Linear models	553
18.4.2	Nonlinear models	554
Part IV Appendices		555
Appendix 1 Data on engineering properties of materials used and made by the confectionery industry		557
A1.1	Carbohydrates	557
A1.2	Oils and fats	566
A1.3	Raw materials, semi-finished products and finished products	567
Appendix 2 Solutions of sucrose, corn syrup and other monosaccharides and disaccharides		579
Appendix 3 Survey of fluid models		582
A3.1	Decomposition method for calculation of flow rate of rheological models	582
A3.1.1	Principle of the decomposition method	582
A3.1.2	Bingham model	583
A3.1.3	Casson model ($n = 1/2$)	585
A3.1.4	Peek, McLean and Williamson model	586
A3.1.5	Reiner-Philippoff model	587
A3.1.6	Reiner model	587
A3.1.7	Rabinowitsch, Eisenschitz, Steiger and Ory model	588
A3.1.8	Oldroyd model	589
A3.1.9	Weissenberg model	590
A3.1.10	Ellis model	591

A3.1.11	Meter model	591
A3.1.12	Herschel–Bulkley–Porst–Markowitsch–Houwink (HBPMH) (or generalized Ostwald–deWaele) model	592
A3.1.13	Ostwald–de Waele model	594
A3.1.14	Williamson model	595
A3.2	Calculation of the friction coefficient ξ of non-Newtonian fluids in the laminar region	596
A3.3	Generalization of the Casson model	597
A3.3.1	Theoretical background to the exponent n	597
A3.3.2	Theoretical foundation of the Bingham model	598
A3.4	Determination of the exponent n of the flow curve of a generalized Casson fluid	598
A3.5	Dependence of shear rate on the exponent n in the case of a generalized Casson fluid	600
A3.6	Calculation of the flow rate for a generalized Casson fluid	601
A3.7	Lemma on the exponent in the generalized Casson equation	603
	Further reading	605
Appendix 4 Fractals		606
A4.1	Irregular forms – fractal geometry	606
A4.2	Box-counting dimension	606
A4.3	Particle-counting method	607
A4.4	Fractal backbone dimension	608
	Further reading	608
Appendix 5 Introduction to structure theory		609
A5.1	General features of structure theory	609
A5.2	Attributes and structure: A qualitative description	610
A5.3	Hierarchical structures	611
A5.4	Structure of measures: A quantitative description	611
A5.5	Equations of conservation and balance	612
A5.6	Algebraic structure of chemical changes	614
A5.7	The technological triangle: External technological structure	614
A5.8	Conserved substantial fragments	615
Appendix 6 Technological lay-outs		617
	Further reading	629
<i>References</i>		630
<i>Index</i>		668