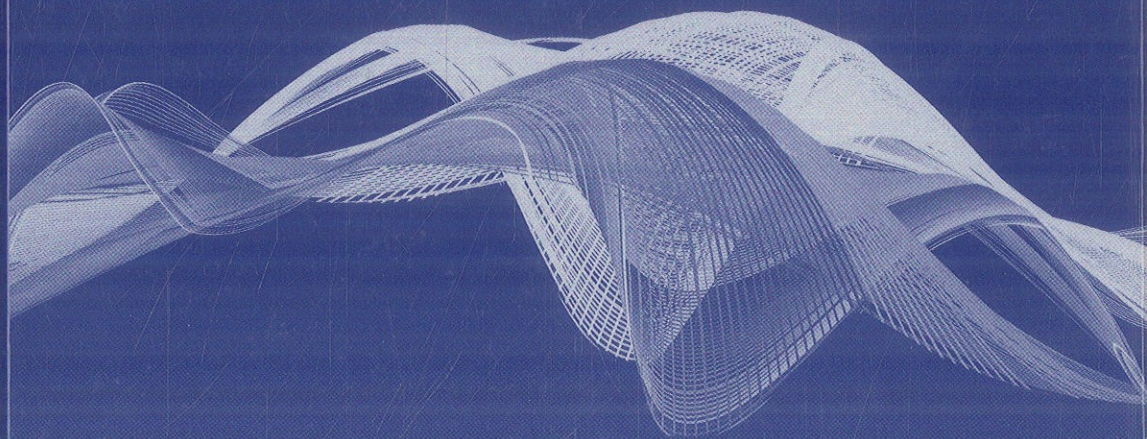


SERIES IN HIGH ENERGY PHYSICS, COSMOLOGY, AND GRAVITATION

The Standard Model and Beyond



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