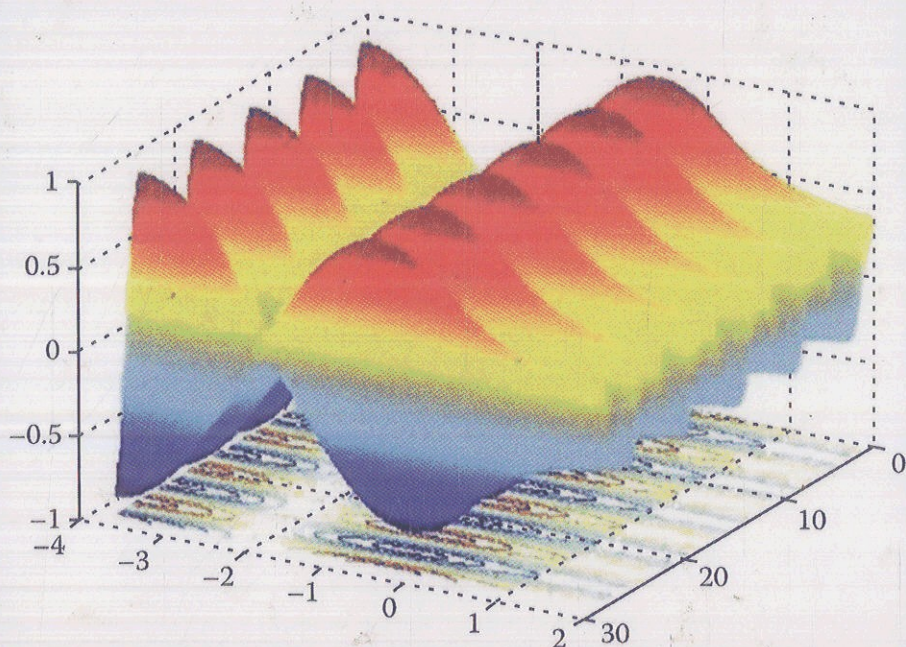


SECOND EDITION

ELECTROMAGNETICS

OF TIME VARYING COMPLEX MEDIA

Frequency and Polarization Transformer



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